Target Tracking Le 5: Multi-Target Tracking: multi-hypothesis tracking

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Summary: lecture 4

- 1 Multi-Hypothesis Tracking
- 2 Conceptual MHT
- 3 Hypothesis-Oriented MHT
- 4 Track-Oriented MHT
- 5 Exercises



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R. Karlsson

Sensor

Detection Association STT Throck/Hypothesis logic

Track/Hypothesis logic

Presentation

- Extended previous methods to several targets.
- Methods for gating, clustering, and association were presented, yielding the validation and association matrix.
- SHT: One measurement association hypothesis is used
 - GNN: A hard decision; choose the most likely association hypothesis.
 - The association problem can be solved with many of-the-shelf algorithms, e.g., auction, after constructing the association (cost) matrix.
 - JPDA: A soft decision; marginalize all possible associations.

 How to combine the possible measurements depends on the association matrix.

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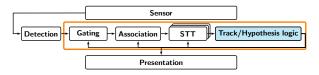
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Multi-Hypothesis Tracking





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Y_t Hypotheses gen. SHT Using given hyp. Hypotheses prob. Pruning Hypotheses red. Pruning Merging $\theta_{1:t}$

An MHT can conceptually be seen as:

- Generating all possible association hypotheses.
- Run an SHT for each potential association.
- Compute the probability of the different options.
- Reduce the number of hypothesis to make the algorithms manageable.

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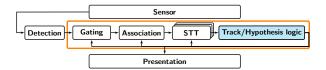
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Multiple Hypothesis Tracking (MHT)

- MHT: consider multiple associations hypotheses over time, *i.e.*, difficult decisions are postponed until more data available.
- MHT took off with the seminal paper (Reid, 1979).
- There were MHT solutions before Reid's, but not as efficient.
- Integrated track initialization.
- Two principal implementations:
 - Hypotheses-oriented (HO-MHT)
 - Track-oriented (TO-MHT)
- TO-MHT was at some point considered more efficient, but HO-MHT can now be quite efficiently implemented.

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The Conceptual MHT Principle





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Conceptual MHT: basic idea

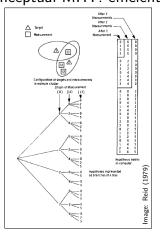
Idea

Generate all possible hypotheses, and then prune to avoid combinatorial hypotheses growth.

- Described by Reid (1979).
- Intuitive hypothesis based *brute force* implementation.
- Between consecutive time instants, different association hypotheses are kept in memory.
- Hypothesis limiting techniques:
 - Prune low probability hypotheses.
 - \blacksquare N-scan pruning.
 - Merge similar hypotheses.



Conceptual MHT: efficient implementation



- Reid (1979): list with hypothesis.
- One measurement for each track.
- Gating to remove unlikely combinations.
- Clustering could be used to split the problem in simpler ones.

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Hypothesis Probabilities (from last lecture on SHT)

Consider association hypotesis θ_t in measurement scan Y_t .

$$p(\theta_t|Y_t) \propto (\beta_{\mathrm{FA}})^{m_t^{\mathrm{FA}}} (\beta_{\mathrm{NT}})^{m_t^{\mathrm{NT}}} \Big[\prod_{j \in \mathcal{J}} P_{\mathrm{D}} p_{t|t-1}^{(j)} \big(y_t^{(\theta_t^{-1}(j))} \big) \Big] \Big[\prod_{j \in \bar{\mathcal{J}}} (1 - P_{\mathrm{D}} P_{\mathrm{G}}) \Big],$$

where

- Measurement to track association at time t: θ_t
- \mathcal{J} is the set of indices of detected tracks (assigned).
- $\bar{\mathcal{J}}$ is the set of indices of non-detected tracks (not assigned).
- $\theta_t^{-1}(j)$ is the index of the measurement that is assigned to track $j \in \mathcal{J}$. $(\theta_t^{-1}(j) = \emptyset$ is shorthand for no measurement associated with track j.)
- All but the last factors are associated with a measurement.

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Extended Notation to Handle MHT

- One measurement sequence: $y_{1:t} = \{y_1, y_2, \dots, y_t\}.$
- Measurements in a scan: $Y_t = \{y_t^{(1)}, y_t^{(2)}, \dots, y_t^{(m_t)}\}$
- $Y_{1:t} = \{Y_1, Y_2, \dots, Y_t\}$
- ullet The set of measurement to track association at time t: $heta_t$
- Hypothesis i at time $t: \theta_t^{(i)}$.
- $\theta_{1:t}$ is the history of measurement to track associations.
- ullet Between consecutive time instants, N_h different association hypotheses, $\{\theta_{1:t-1}^{(i)}\}_i$, are kept in memory.
- $\theta_{1:t}^{(ij)} = (\theta_{1:t-1}^{(i)}, \theta_{t}^{(j)})$

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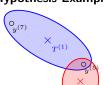
Generating Hypotheses

- Assume the hypotheses from time t-1, $\{\theta_{1\cdot t-1}^{(i)}\}_{i}$.
- Form all possible new hypotheses,

$$\theta_{1:t}^{(ij)} = (\theta_{1:t-1}^{(i)}, \theta_t^{(j)}),$$

with the obtained measurements, Y_t .

I.e., each measurement should be assigned either to an existing track, create a new track, or be considered a false detection.



Hypothesis: $\theta_{1:t-1}^{(1)}$





Hypothesis Example

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Complexity Reduction

The number of different hypotheses to consider grows exponentially over time, as has been illustrated, and guickly becomes intractable. Tricks and approximations necessary to obtain a realistic problem.

Complexity reducing method:

- Clustering (as studied before, always fundamental).
- Pruning of low probability hypotheses.
- N-scan pruning.
- Merging of similar hypotheses.

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Hypothesis Probabilities

Now, let $\theta_{1:t}^{(ij)} = \{\theta_{1:t-1}^{(i)}, \theta_t^{(j)}\}$, then applying Baye's rule and $Y_{1:t} = \{Y_t, Y_{1:t-1}\}$

$$\begin{split} p(\theta_{1:t}^{(ij)}|Y_{1:t}) &= p(Y_t|\theta_{1:t}^{(ij)},Y_{1:t-1})p(\theta_{1:t}^{(ij)}|Y_{1:t-1}) \\ &= p(Y_t|\theta_{1:t}^{(ij)},Y_{1:t-1})p(\theta_t^{(j)}|\theta_{1:t-1}^{(i)},Y_{1:t-1})p(\theta_{1:t-1}^{(i)}|Y_{1:t-1}) \\ &\propto \beta_{\text{FA}}^{m_t^{\text{FA}}} \beta_{\text{NT}}^{m_t^{\text{NT}}} \bigg[\prod_{k \in \mathcal{I}^{(j)}} P_{\text{D}} p_{t|t-1}^{(k)} (y_t^{((\theta_t^{(j)})^{-1}(k))}) \bigg] \bigg[\prod_{k \in \bar{\mathcal{I}}^{(j)}} (1 - P_{\text{D}} P_{\text{G}}) \bigg] p(\theta_{1:t-1}^{(i)}|Y_{1:t-1}) \end{split}$$

Note

The sets $\mathcal{J}^{(j)}$ and $\bar{\mathcal{J}}^{(j)}$ depend on $\theta_{1,t-1}^{(i)}$! The number of targets and target estimates usually differ between hypotheses.

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Complexity Reduction: pruning

 Delete hypotheses with low probability Delete hypotheses with probability below a threshold, γ_p (e.g., $\gamma_p = 0.1\%$):

Deletion Condition: $p(\theta_{1:t}^{(i)}) < \gamma_n$

• Keep only the most probable hypotheses

Keep the most probable hypotheses that together make up enough of the total probability mass, γ_c (e.g., $\gamma_c = 99\%$):

Deletion Condition:
$$i > i_{\mathsf{th}} = \arg\min_{i} \sum_{k=1}^{i} p(\theta_{1:t}^{(k)}) \geq \gamma_{c},$$

where $\theta_{1:t}^k$ has been ordered such that $p(\theta_{1:t}^{(k)}) \geq p(\theta_{1:t}^{(k+1)})$

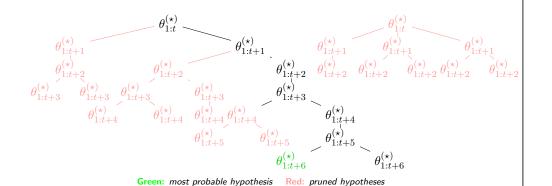
Make sure to renormalize the hypothesis probabilities after pruning.



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Complexity Reduction: N-Scan Pruning



 ${\cal N}=2\text{-scan}$ pruning: Only keep the most likely node ${\cal N}$ steps back

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Reid's original paper suggests to check for hypothesis pairs with:

- the same number of targets (tracks)
- similar track estimates

If these conditions are satisfied:

- merge the hypotheses
- assign the new hypothesis the sum of the combined hypotheses' probability

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Conceptual MHT: summary

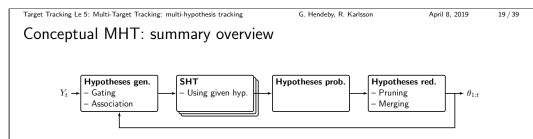
- Attractive method since each hypothesis is:
 - an alternative representation of reality
 - easily interpreted
- Drawback: generating all possible hypotheses only to discarding (most of) them is inefficient.
- Some hypotheses contain the same track; hence fewer unique tracks than hypotheses.

Extensions of the original MHT idea

HO-MHT More clever/efficient hypotheses generation: Cox and Miller (1995).

TO-MHT Track oriented hypothesis handling.

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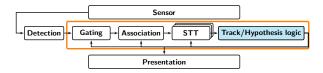


An MHT can conceptually be seen as:

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Hypothesis-Oriented Multiple-Hypothesis Tracker





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Hypothesis-Based MHT

- Proposed by Cox and Miller (1995).
- Only generate the best hypotheses, ignore hypotheses that will anyhow be deleted.
- Propagate the N_h -best hypotheses:
 - Generating as few unnecessary hypothesis as possible.
 - \blacksquare Use the k-best algorithm to find solutions to the assignment problem.
- Regular hypothesis reduction techniques still apply.

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Assignment Problem: *k*-best solutions

Murty's method

Given the assignment matrix A:

- Find the best solution to the assignment problem (e.g., Auction).
- For i = 2, ..., k, or until there are no more solutions to evaluate:
 - Construct new assignment problems by, in turn excluding each of the assignments made in the $(i-1)^{th}$ solution.
 - Find the best solution to each of these problems (e.g., Auction).
 - The i^{th} best assignment is the solution giving the maximum reward (minimum cost) among all solutions evaluated so far that have not been picked.

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HO-MHT: algorithm outline

Aim: Given N_h hypotheses $\{\theta_{1:t-1}^{(i)}\}_i$ and measurements $Y_t = \{y_t^{(k)}\}_{k=1}^{m_t}$, find the N_h best hypotheses $\{\theta_{1:t}^{(ij)}\}_{ij}$ (without generating all hypotheses).

Recall: Hypothesis Probability

$$p(\theta_{1:t}^{(ij)}|Y_{1:t}) \propto \beta_{\mathrm{FA}}^{m_t^{\mathrm{FA}}} \beta_{\mathrm{NT}}^{m_t^{\mathrm{NT}}} \bigg[\prod_{k \in \mathcal{J}^{(j)}} \frac{P_{\mathrm{D}} p_{t|t-1}^{(k)} (y_t^{(\theta_t^{(j)})^{-1}(k)})}{1 - P_{\mathrm{D}} P_{\mathrm{G}}} \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior information}} \\ C_i = \prod_{k \in \mathcal{J}^{(j)} \cup \bar{\mathcal{J}}^{(j)}} (1 - P_{\mathrm{D}} P_{\mathrm{G}}) \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior information}} \\ C_i = \prod_{k \in \mathcal{J}^{(j)} \cup \bar{\mathcal{J}}^{(j)}} (1 - P_{\mathrm{D}} P_{\mathrm{G}}) \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior information}} \\ C_i = \prod_{k \in \mathcal{J}^{(j)} \cup \bar{\mathcal{J}}^{(j)}} (1 - P_{\mathrm{D}} P_{\mathrm{G}}) \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior information}} \\ \underbrace{C_i = \prod_{k \in \mathcal{J}^{(j)} \cup \bar{\mathcal{J}}^{(j)}} (1 - P_{\mathrm{D}} P_{\mathrm{G}})}_{\text{Prior information}} \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior information}} \\ \underbrace{C_i = \prod_{k \in \mathcal{J}^{(j)} \cup \bar{\mathcal{J}}^{(j)}} (1 - P_{\mathrm{D}} P_{\mathrm{G}})}_{\text{Prior information}} \bigg] \underbrace{C_i p(\theta_{1:t-1}^{(i)}|Y_{1:t-1})}_{\text{Prior inform$$

- Find the N_h hypotheses $\{\theta_{1:t}^{(ij)}\}_{ij}$ that maximizes $p(\theta_{1:t}^{(ij)}|Y_{1:t})$.
 - Obtain the solution from the assignment (Murty's method).
 - Multiply the obtained quantity by previous hypothesis dependent terms.



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Generating the N_b -best Hypotheses

 $\begin{array}{ll} \textbf{Input} & \{\theta_{1:t-1}^{(i)}\}_i, \ \{P(\theta_{1:t-1}^{(i)}|Y_{0:t-1})\}_i, \ \text{and} \ \{y_t^{(k)}\}_{k=1}^{m_t} \\ \textbf{Output} & \text{HYP-LIST (N_h hypotheses, decreasing probability)} \\ & \text{PROB-LIST (matching probabilities)} \end{array}$

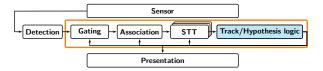
- 1. Initialize all elements in HYP-LIST and PROB-LIST to \emptyset and -1, respectively.
- 2. Compute the assignment matrices $\{\mathcal{A}^{(i)}\}_{i=1}^{N_h}$ for $\{\theta_{1:t-1}^{(i)}\}_{i=1}^{N_h}$
- 3. For $i = 1, ..., N_h$

For $j = 1, \ldots, N_h$

- i). For the assignment matrix $\mathcal{A}^{(i)}$ find the j^{th} best solution $\theta_{1:t}^{(ij)}$.
- ii). Compute the probability $p(\theta_{1:t}^{(ij)})$.
- iii). Update HYP-LIST and PROB-LIST: If the new hypothesis enters the list, discard the least probable entry.
- iv). If $p(\theta_{1:t}^{(ij)})$ is lower than the lowest probability in PROB-LIST discard $\theta_{1:t}^{(ij)}$ and never use $\mathcal{A}^{(i)}$ again in subsequent recursions.



Track Oriented Multiple-Hypothesis Tracker





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Track-Based MHT: motivation

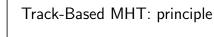
- There are usually more hypotheses than tracks.
- Typically, hypotheses usually contain identical tracks significantly fewer tracks than hypotheses.
- Instead of hypotheses try to build the MHT from tracks:
 - First: consider all track updates within the gating region.
 - Later: impose the usual constraint; one measurement to one track.

Note: hypotheses are generated as needed each time from the tracks.

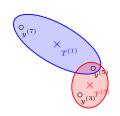
Idea

Store tracks, $T^{(i)}$, not hypotheses, $\theta_{1:t}^{(j)}$, over time.





- Tracks at time t, $\{T_t^{(i)}\}_i$
- Track scores, $Sc(T_t^{(i)})$
- $\bullet\,$ Form a track tree, not a hypothesis tree
- Delete tracks with low scores



 $T_{t}^{(1)} \underbrace{ \begin{array}{c} T_{t+1}^{(1)} \\ T_{t+1}^{(10)} \end{array}}_{T_{t+1}^{(10)}} T_{t+1}^{(10)} \\ T_{t+1}^{(10)} \underbrace{ \begin{array}{c} y^{(3)} T_{t+1}^{(23)} \\ y^{(5)} T_{t+1}^{(25)} \end{array}}_{t+1} T_{t+1}^{(20)} \\ \underbrace{ \begin{array}{c} y^{(3)} T_{t+1}^{(20)} \\ T_{t+1}^{(3)} \end{array}}_{y^{(7)} - (7)} T_{t+1}^{(5)} \end{array} }_{t+1}$



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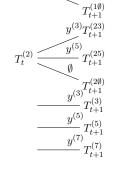
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Track-Based MHT: hypotheses generation

- Hypothesis: a collection of compatible tracks: $\boldsymbol{\theta}_{1:t+1}^{(1)} = \{T_{t+1}^{(17)}, T_{t+1}^{(25)}\}, \quad \boldsymbol{\theta}_{1:t+1}^{(2)} = \{T_{t+1}^{(1\emptyset)}, T_{t+1}^{(25)}, T_{t+1}^{(3)}, T_{t+1}^{(7)}\}$
- Generating hypothesis is needed for reducing the number of tracks further and for user presentation
- Use only tracks with high score
- Keep track compatibility information (e.g., in a binary matrix)

		- 3			(- 6 /			,	,
	$T_{t+1}^{(15)}$	$T_{t+1}^{(17)}$	$T_{t+1}^{(1\emptyset)}$	$T_{t+1}^{(23)}$	$T_{t+1}^{(25)}$	$T_{t+1}^{(2\emptyset)}$	$T_{t+1}^{(3)}$	$T_{t+1}^{(5)}$	$T_{t+1}^{(7)}$
$T_{t+1}^{(15)}$	0	0	0	1	0	1	1	0	1
$T_{t+1}^{(17)}$		0	0	1	1	1	1	1	0
$T_{t+1}^{(1\emptyset)}$			0	1	1	1	1	1	1
$T_{t+1}^{(23)}$				0	0	0	0	1	1
$T_{t+1}^{(25)}$					0	0	1	0	1
$T_{t+1}^{(2\emptyset)}$						0	1	1	1
$T_{t+1}^{(3)}$							0	1	1
$T_{t+1}^{(5)}$								0	1
$T_{t+1}^{(7)}$	1								0





Track Scores and Hypotheses Probabilities

• Track probability:

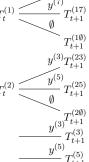
$$P(T_t^{(i)}) = \sum_{T_t^{(i)} \in \theta_{1:t}^{(j)}} P(\theta_{1:t}^{(j)})$$

Hypothesis score:

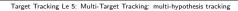
$$\operatorname{Sc}(\theta_{1:t}^{(i)}) = \sum_{T_t^{(j)} \in \theta_{1:t}^i} \operatorname{Sc}(T_t^{(j)})$$

Hypothesis probability:

$$P(\theta_{1:t}^{(i)}) = \frac{\exp\left(\operatorname{Sc}(\theta_{1:t}^{(i)})\right)}{1 + \sum_{j} \exp\left(\operatorname{Sc}(\theta_{1:t}^{(j)})\right)}$$



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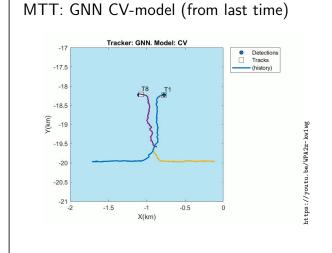
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Complexity Reducing Techniques

- Cluster incompatible tracks for efficient hypothesis generation
- ullet Apply N-scan pruning to the track trees
- Merge tracks with common recent measurement history



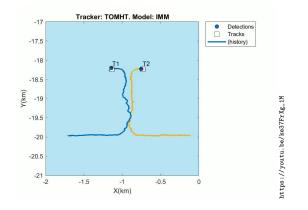
- Global nearest neighbor (GNN) tracker
- Simple constant velocity (CV) model
- Note the label switch and that one of the tracks is lost half way, and restarted as a new one.

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- Multi-hypothesis tracker (MHT) resolves measurement ambiguities
- Interacting multiple models (IMM) better captures the mixed level of agility



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Which MTT Method to Use?

SNR	Low	Medium	High
Low	Group TT / PHD	GNN	GNN
Medium	MHT	GNN or JPDA	GNN
High	TrBD / MHT	MHT	Any

- GNN and JPDA are very bad in low SNR.
- When using GNN, one generally has to enlarge the overconfident covariances to account for neglected data association uncertainty.
- JPDA has track coalescence and should not be used with closely spaced targets, see the "coalescence avoiding" versions.
- MHT requires significantly higher computational load but it is said to be able to work reasonably under 10-100 times worse SNR.

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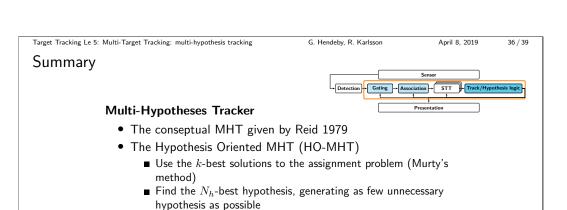
User Presentation Logic

- Maximum probability hypothesis: simplest alternative.
 - Possibly jumpy; the maximum probability hypothesis can change erratically.
- Show track clusters: (weighted) mean, covariance and expected number of targets.
- Keep a separate track list: update at each step with a selection of tracks from different hypotheses.
- Consult (Blackman and Popoli, 1999) for details.



Summary





- Track Oriented MHT (TO-MHT)
 - Maintain tracks, create hypotheses when needed.
 - Less tracks than global hypotheses.
- Presentation of the current state is not trivial.



Exercises



Target Tracking Le 5: Multi-Target Tracking: multi-hypothesis tracking G. Hendeby, R. Karlsson April 8, 2019 38 / 39 Exercise 3 1. Apply the MHT to the simulated scenario from previous exercise Simulate trajectory 1800 • Generate measurement: 1600 1400 $\blacksquare P_{\rm D}$ \blacksquare P_{FA} ■ clutter • Details specificed in the previous exercise Murty's method provided Note: see separate exercise document. LINKÖPING UNIVERSITY

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Exercise 3

- 2. Apply the MHT to the mysterious data set from previous exercise
- MHT
- Compare with JPDA, GNN tracking.

Details specificed in the previous exercise.

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