

Target Tracking

Le 1: Introduction

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Course Information

Multi-Target Tracking Course, Spring 2019

Aim

The aim of the course is to provide an introduction to *multi-target tracking* (MTT); both theoretical and practical aspects. After the course a student should be able to explain the basic ideas underlying MTT and feel confident to implement the fundamental methods.

Course activities:

- 8 lectures where the theoretical aspects of MTT are explained
- 1 guest lecture; Veoneer, where we hear from their tracking specialists
- Practical coding exercises, performed on your own
- Project work

Responsible:

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- Rickard Karlsson (rickard.g.karlsson@liu.se)

Course homepage:

- <http://www.control.isy.liu.se/student/graduate/targettracking>

Course Content

- Single-target tracking (STT)
- Motion and sensor models:
 - Common tracking models
 - Maneuvering targets (IMM)
 - Clutter
- Multi-target tracking (MTT):
 - Association
 - Track logic
 - Global Nearest Neighbor (GNN) Tracker
 - Multi-Hypotheses Tracker (MHT)
- Outlook, modern methods:
 - Track before detect (TrBD)
 - RFS/FISST: Probability hypothesis density (PHD), Multi-Bernoulli
 - Track-to-track fusion (T2TF)

Course Examination

Three independent parts with different focuses:

1. Basic theory and understanding: **exam** (2 hp)
Theory is examined in a brief written exam.
2. Implementation and practice: **exercises** (4 hp)
Implementation skill and practical knowhow are examined using assignments during the course.
3. Research related work: **project** (3 hp)
Use course skills extensions on the topic for a larger tracking project, preferably related to your research. Individually or in a group of two.

Course Prerequisites

Familiarity with:

- Basic knowledge of probability theory
- State-space models
- Bayesian estimation methods
 - Kalman filter (KF)
 - Extended Kalman filter (EKF)
 - Unscented Kalman filter (UKF)
 - Particle filter (PF)
- Coding in MATLAB or similar (for the exercises)

Suitable background material

- Sensor Fusion course (TSRT14): <http://www.control.isy.liu.se/student/tsrt14>
- F. Gustafsson, L. Ljung, and M. Millnert. *Signal processing*. Studentlitteratur, 1. edition, 2010.
- F. Gustafsson. *Statistical Sensorfusion*. Studentlitteratur, 3. edition, 2018.
- T. Kailath, A. H. Sayed, and B. Hassibi. *Linear Estimation*. Prentice-Hall, Inc, 2000. ISBN 0-13-022464-2.
- S. M. Kay. *Fundamentals of Statistical Signal Processing: Estimation Theory, volume 1*. Prentice-Hall, Inc, 1993. ISBN 0-13-042268-1.

Lecture Schedule (preliminary)

Le	Topic	Date	Ex
1	Introduction	Jan 15	10–12
2	Models for Target tracking	Jan 25	13–15
3	Single target tracking	Feb 1	13–15 Ex 1
4	Multi-target tracking (1/2): GNN, JPDA	Feb 27	Ex 2
5	Multi-target tracking (2/2): MHT	Apr 3	Ex 3
6	Random Finite Sets: PHD, etc	Apr 17	
7	Guest lecture: Veoneer	May	(Ex 4)
8	Various topics (TrBD, T2T, ETT)	May	
9	Project Presentations	Aug	

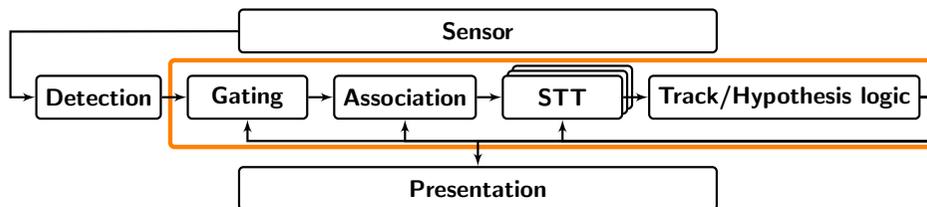
- Lectures are in **Algotimen** unless otherwise stated.
- Exercises are due the Sunday before the next lecture.
- Dates are preliminarv. check homepage and mails for updates.

Course Literature

- Selected papers handed out during the course will be enough to follow the course.
- For a fairly complete overview of the target tracking problem, methods, and algorithm collected in one place, the following books are good entry points.
 - S. S. Blackman and R. Popoli. *Design and analysis of modern tracking systems*. Artech House radar library. Artech House, Inc, 1999. ISBN 1-5853-006-0.
 - Y. Bar-Shalom, P. Willett, and T. Xin. *Tracking and Data Fusion: A Handbook of Algorithms*. Yaakov Bar-Shalom Publishing, 2011. ISBN 0-9648-3-127-9.

Multi-Target Tracking Overview

Multi-Target Tracking: conceptual view

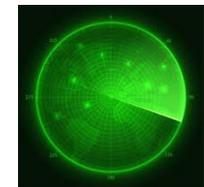
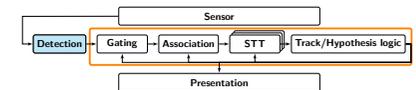


Components

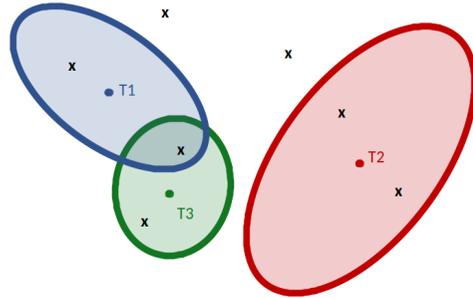
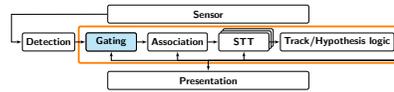
1. Detections/Observations
2. Gating
3. Association
4. Single-target tracking
5. Track and hypothesis logics
6. Presentation

Multi-Target Tracking: detection

- Considered done in this course
- Sensor level signal processing
- Heavily sensor dependent

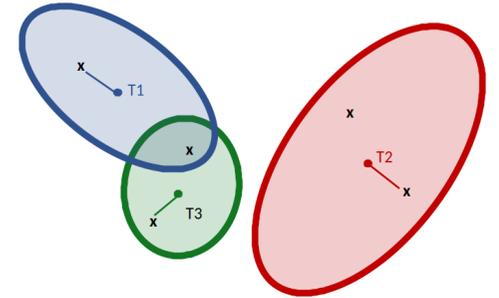
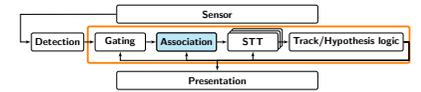


Multi-Target Tracking: gating



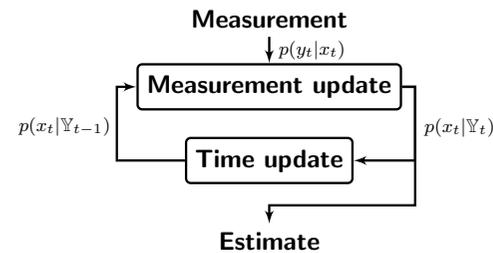
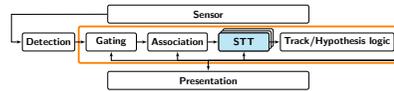
- Determine which measurements could come from known targets
- Reduce tracking complexity

Multi-Target Tracking: association



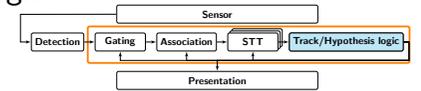
- Match observations to targets
- One or many different associations

Multi-Target Tracking: STT

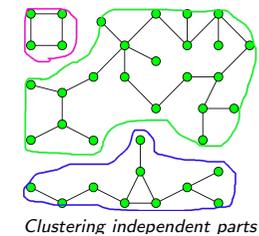


- Perform for each target independently, given associated measurements
- Standard methods: EKF, UKF, PF, ...
- Yields state and uncertainty, given the association hypothesis

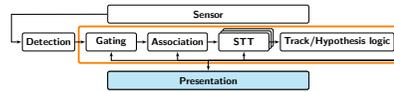
Multi-Target Tracking: track/hypothesis logic



- Compute probability of given track/association hypothesis
- Track management: birth, death
- Clustering for efficiency



Multi-Target Tracking: presentation



- How to present the result?
- Not addressed in the course



Tracking Examples

Selected examples

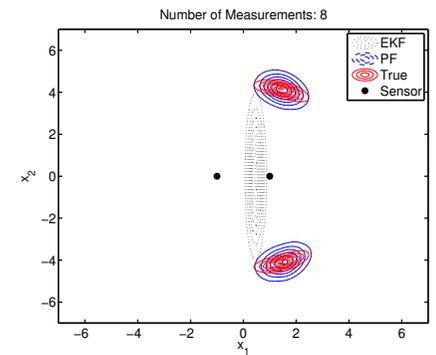
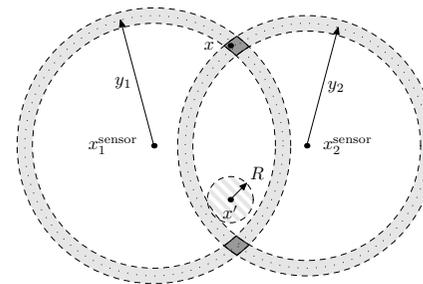
Selected examples (single target tracking/filtering and multiple target tracking):

- STT** Range-only measurements
- STT** Positioning based on a tracking sensor
- STT** Multiple models for maneuvering target tracking (IMM)
- STT** Track before detect
- MTT** Nearest Neighbor CV-model
- MTT** MHT
- MTT** PHD-filtering

STT: Range-Only Tracking

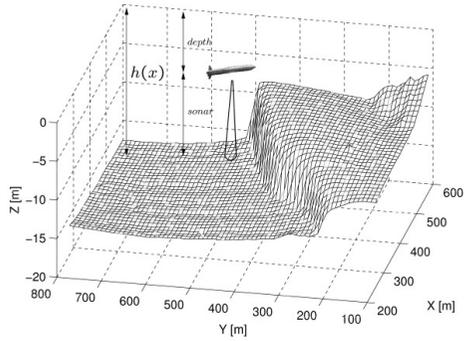
Range-Only Measurement

Performance, and performance measures for RO:



STT: UW map-aided navigation

UW navigation



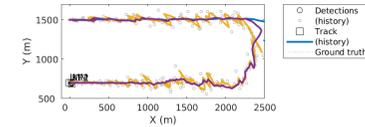
<https://youtu.be/J3UjVEn87yE>

- Underwater vessel measures its own depth and distance to bottom, and sea chart provides depth $h(x_t)$.
- Video shows how a uniform prior quickly converges to a unimodal particle cloud. Note how the cloud changes form when passing the ridge.

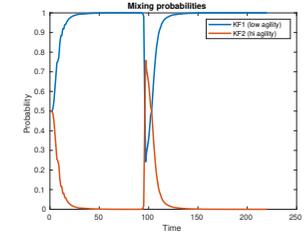
STT: Maneuvering Target

The IMM method for two models

A radar tracking application is presented using the IMM method with two filters. One filter is used to handle a straight flying path accurately, whereas the other is used to manage maneuvers. Due to the non-linearities in the measurement equation an EKF is used for the estimation.



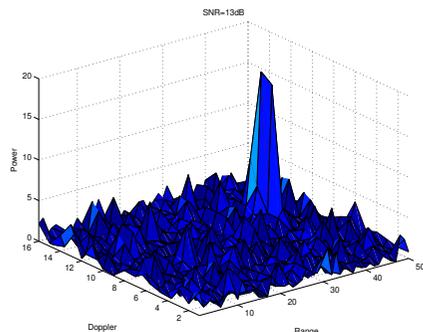
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STT: Track-Before-Detect (TrBD)

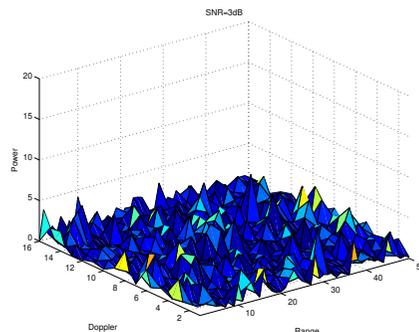
Track without first detecting the target

SNR=13 dB



Easy to detect a point target.

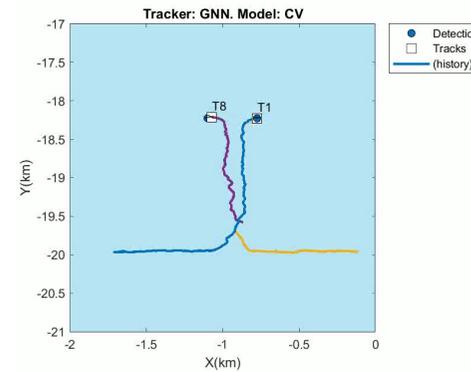
SNR=3 dB



Hard to detect a point target.

MTT: GNN CV-model

Global nearest neighbor tracking



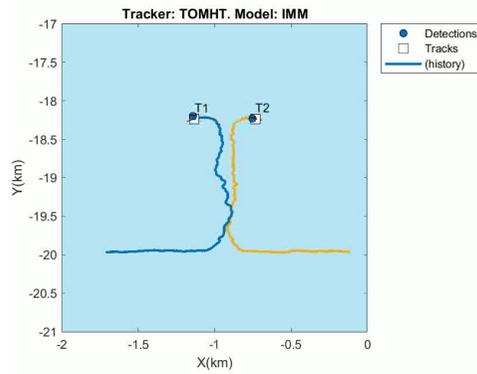
<https://youtu.be/WPA2z-kv1wG>

- *Global nearest neighbor* (GNN) tracker
- Simple *constant velocity* (CV) model
- Problems handling the mixed level of agility

MTT: MHT IMM

Multi-hypothesis tracking

- *Multi-hypothesis tracker* (MHT) resolves measurement ambiguities
- *Interacting multiple models* (IMM) better captures the mixed level of agility

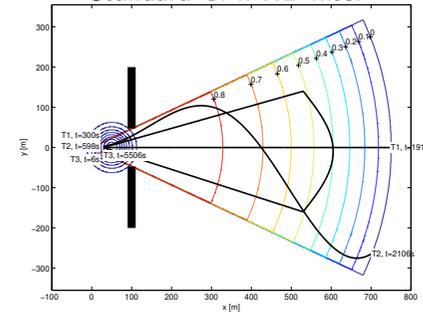


https://youtu.be/ke37FzXg_1M

MTT: PHD Filter Example

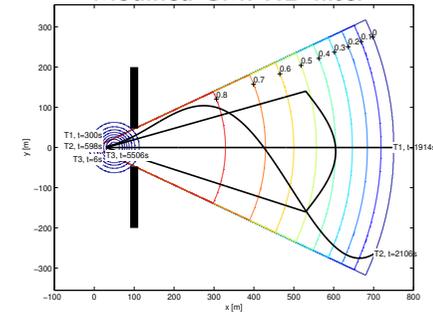
Random finite set tracking

Standard GMPHD filter



<https://youtu.be/PJimgB83X88>

Modified GMPHD filter



<https://youtu.be/cAL3yurVZAK>

- Probability of detection dies off as a 3rd-degree polynomial, inspired by real data

Tracking Preliminaries

Introduction to Target Tracking (TT)

Definition: Target

A **target** is anything whose state (x) is of interest to us.

- The state can change over time with a dynamics which is itself unknown.
- Measurement/detections/observations (y^i) comes from uncertain origin.
- There are false observations, $P_{FA} > 0$.
- Some measurements are missing, $P_D < 1$.
- Generally have no initial guess or estimate of the target state.

Definition: Target tracking

Target tracking, in its most general and abstract form, is a special case of dynamic estimation theory.

Targets and Tracks

Definition: Track

A **track** is a sequence of measurements that has been decided or hypothesized by the tracker to come from a single source.

- Usually, instead of the list of actual measurements, sufficient statistics is held e.g., mean and covariance in the case of a KF, particles in the case of a PF.
- Generally each arriving measurement must start a track. Hence tracks must be classified, but must not be treated equally.

Target Types

Point target A target that can result in at most a single measurement.

- This means its magnitude is comparable to sensor resolution.
- However, an extended target can also be treated as a point target by tracking its centroid or corners.

Extended target A target that can result in multiple measurements in a single scan.

Unresolved targets This denotes a group of close targets that can collectively result in a single measurement in the sensor.

Dim target This is a target whose magnitude is below sensor resolution. These can be tracked much better with *track before detect* (TrBD) type approaches.

Bayesian Problem Formulation and Solution

- The state x_t of interest
- Given measurements/observations

$$\mathbb{Y}_t = \{y_1, \dots, y_t\}$$

- System model:

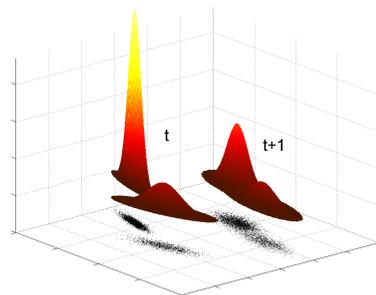
$$x_t = f(x_{t-1}, w_{t-1}) \quad \longleftrightarrow \quad p(x_t | x_{t-1})$$

$$y_t = h(x_t) + e_t \quad \longleftrightarrow \quad p(y_t | x_t)$$

where w_{t-1} and e_t are stochastic processes

- Bayesian solution

$$p(x_t | \mathbb{Y}_t) = \int \frac{p(y_t | x_t) p(x_t | x_{t-1}) p(x_{t-1} | \mathbb{Y}_{t-1})}{p(y_t | \mathbb{Y}_{t-1})} dx_{t-1}$$



Bayesian Framework for Estimation

- Bayesian solution

$$p(x_t | \mathbb{Y}_{t-1}) = \int p(x_t | x_{t-1}) p(x_{t-1} | \mathbb{Y}_{t-1}) dx_{t-1} \quad (\text{TU})$$

$$p(x_t | \mathbb{Y}_t) = \frac{p(y_t | x_t) p(x_t | \mathbb{Y}_{t-1})}{p(y_t | \mathbb{Y}_{t-1})} \quad (\text{MU})$$

- Two stage procedure:

- Time update (TU): Predict the future
- Measurement update (MU): Correct prediction based on observations

- Only a few analytic solutions:

- Linear Gaussian model \Rightarrow Kalman filter (KF)
- Hidden Markov model (HMM)

- In most cases approximations are needed:

- Analytic
- Stochastic

Filtering

Common filters used for tracking:

- *Kalman filter* (KF)
- *Extended Kalman filter* (EKF)
- *Unscented Kalman filter* (UKF)
- *Particle filter* (PF)
- Filter banks, e.g., *interacting multiple models* (IMM)

We will assume basic knowledge of first and only give a brief introduction here. Next lecture will deal with models used in tracking, and filter banks.

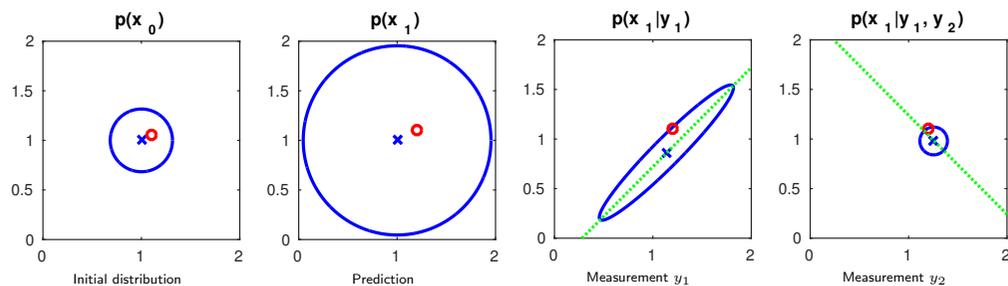
Kalman Filter (KF)

- Probably the most used filter in practice.
- Applies to linear state-space models:

$$\begin{aligned} x_{t+1} &= F_t x_t + G_t w_t, & \text{cov}(w_t) &= Q_t \\ y_t &= H_t x_t + e_t, & \text{cov}(e_t) &= R_t \end{aligned}$$

- Shown to be optimal if the noise is Gaussian, otherwise the best linear unbiased estimator (BLUE).
- Can be implemented efficiently.

Kalman Filter: illustration



Extended Kalman Filter (EKF)

Standard Algorithm

- **Initialization:** $\hat{x}_{0|0} = x_0$ and $P_{0|0} = \Pi_0$.

- **Time update:**

$$\begin{aligned} \hat{x}_{t|t-1} &= f(\hat{x}_{t-1|t-1}) \\ P_{t|t-1} &= F_{t-1} P_{t-1|t-1} F_{t-1}^T + G_{t-1} Q_{t-1} G_{t-1}^T \end{aligned}$$

- **Measurement update:**

$$\begin{aligned} \hat{x}_{t|t} &= \hat{x}_{t|t-1} + K_t (y_t - h(\hat{x}_{t|t-1})) \\ P_{t|t} &= P_{t|t-1} - K_t H_t P_{t|t-1}, \end{aligned}$$

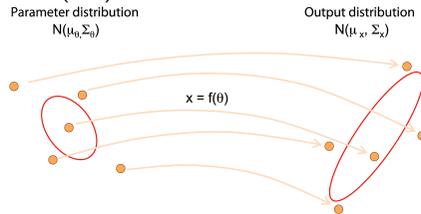
where

$$\begin{aligned} K_t &= P_{t|t-1} H_t^T (H_t P_{t|t-1} H_t^T + R_t)^{-1} \\ f_t^T &= \nabla_x f^T(x) \Big|_{x=\hat{x}_{t|t}}, & H_t^T &= \nabla_x h^T(x) \Big|_{x=\hat{x}_{t|t-1}} \end{aligned}$$

Unscented Kalman Filter (UKF)

Fundamental idea:

Use the unscented transform (UT) to transform stochastic variables when needed.



Generate $2n_x + 1$ *sigma points*, transform these, and fit a Gaussian distribution:

$$\begin{aligned} x^{(0)} &= \hat{x} \\ x^{(\pm i)} &= \hat{x} \pm \sqrt{n_x + \lambda} P_{:,i}^{1/2}, & i = 1, 2, \dots, n_x \\ z^{(i)} &= g(x^{(i)}) \\ E(z) &\approx \sum_{i=-n_x}^{n_x} \omega^{(i)} z^{(i)} & \text{cov}(z) \approx \sum_{i=-n_x}^{n_x} \omega_c^{(i)} (z^{(i)} - E(z))(z^{(i)} - E(z))^T \end{aligned}$$

Unscented Kalman Filter Algorithm (1/2)

Algorithm: time update

$$\begin{aligned} \hat{x}_{t|t-1} &= \sum_{i=0}^N \omega_t^{(i)} x_{t|t-1}^{(i)} \\ P_{t+1|t} &= \sum_{i=0}^N \omega_{c,t}^{(i)} (x_{t|t-1}^{(i)} - \hat{x}_{t|t-1})(x_{t|t-1}^{(i)} - \hat{x}_{t|t-1})^T \\ x_{t|t-1}^{(i)} &= f(x_{t-1|t-1}^{(i)}, w_t^{(i)}) \\ \omega^{(0)} &= \frac{\lambda}{n_x + \lambda} & \omega_c^{(0)} &= \omega^{(0)} + (1 - \alpha^2 + \beta) \\ \omega^{(\pm i)} &= \frac{1}{2(n_x + \lambda)} & \omega_c^{(\pm i)} &= \omega^{(\pm i)} \end{aligned}$$

Unscented Kalman Filter Algorithm (2/2)

Algorithm: measurement update

$$\begin{aligned} \hat{x}_{t|t} &= \hat{x}_{t|t-1} + P_{t|t-1}^{xy} P_{t|t-1}^{-yy} (y_t - \hat{y}_t) \\ P_{t|t} &= P_{t|t-1} - P_{t|t-1}^{xy} P_{t|t-1}^{-yy} P_{t|t-1}^{xyT} \\ y_t^{(i)} &= h(x_{t|t-1}^{(i)}, e_t^{(i)}) \\ \hat{y}_t &= \sum_{i=0}^N \omega_t^{(i)} y_t^{(i)} \\ P_{t|t-1}^{yy} &= \sum_{i=0}^N \omega_{c,t}^{(i)} (y_t^{(i)} - \hat{y}_t)(y_t^{(i)} - \hat{y}_t)^T \\ P_{t|t-1}^{xy} &= \sum_{i=0}^N \omega_{c,t}^{(i)} (x_{t|t-1}^{(i)} - \hat{x}_{t|t-1})(y_t^{(i)} - \hat{y}_t)^T. \end{aligned}$$

Unscented Kalman Filter: design parameters

- λ is defined by $\lambda = \alpha^2(n_x + \kappa) - n_x$.
- α controls the spread of the sigma points and is suggested to be chosen around 10^{-3} .
- β compensates for the distribution, and should be chosen to $\beta = 2$ for Gaussian distributions.
- κ is usually chosen to zero.

Note

- $n_x + \lambda = \alpha^2 n_x$ when $\kappa = 0$.
- The weights sum to one for the mean, but sum to $2 - \alpha^2 + \beta \approx 4$ for the covariance. Note also that the weights are not necessarily in $[0, 1]$.
- The mean has a large negative weight!

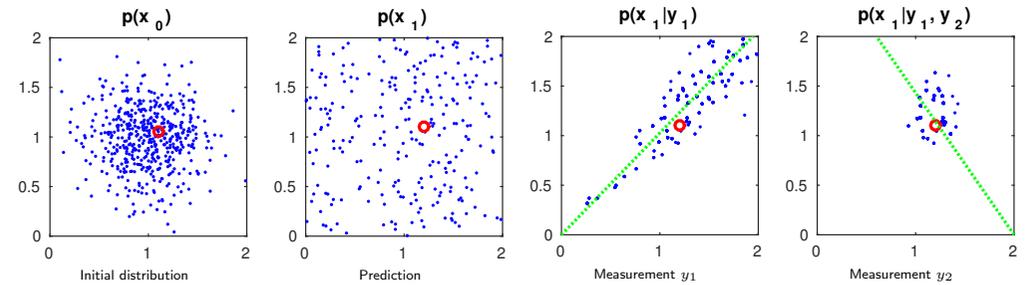
Particle Filter (PF)

Postulate a discrete approximation of the posterior. For the predictive density, we have

$$\hat{p}(x_t | \mathbb{Y}_t) = \sum_{i=1}^N w_{t|t-1}^{(i)} \delta(x_t - x_t^{(i)}).$$

Simulate each particle (sample) independently, and compare how well they match the obtained measurements. Use the law of large numbers.

Particle Filter: illustration



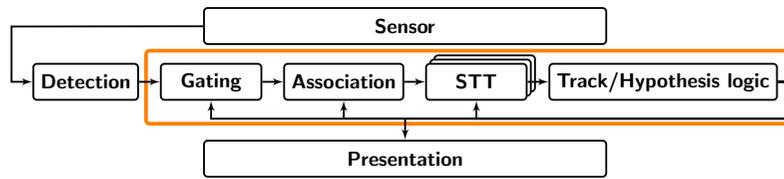
Particle Filter: algorithm

Sampling Importance Resampling (SIR) Algorithm

- **Initialize:** Generate N samples $\{x_{0|0}^{(i)}\}_{i=1}^N$ from $p_{x_0}(x_0)$.
- **Time update:** Simulate new particles, i.e. $x_{t|t-1}^{(i)} = f(x_{t-1|t-1}^{(i)}, w_{t-1}^{(i)})$, $i = 1, \dots, N$, where $w_{t-1}^{(i)} \sim p_w(w_{t-1})$.
- **Measurement update:** Compute the weights $\omega_t^{(i)} \propto p(y_t | x_{t|t-1}^{(i)})$ and normalize so they sum to one, $\sum_i \omega_t^{(i)} = 1$.
- **Resample:** Generate a new set $\{x_{t|t}^{(i)}\}_{i=1}^N$ by resampling with replacement N times from $\{x_{t|t-1}^{(j)}\}_{j=1}^N$, where $\Pr(x_{t|t}^{(i)} = x_{t|t-1}^{(j)}) = \omega_t^{(j)}$.

Summary

Summary



- Multi-target tracking is the problem of decide how many targets are present and how they move, given measurements with imperfections.
- Classic MTT can be divided in several stages: gating, association, single target tracking, track/hypothesis logic, and presentation.
- Single target tracking: Kalman type filters, particle filters

Decide what your ambitions are for the course!