



ROYAL INSTITUTE
OF TECHNOLOGY

Security and Limitations of Cyber-Physical Systems

Lecture 1: Introduction

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August 24-26, 2015

Acknowledgments

- György Dán (KTH)
- Karl Henrik Johansson (KTH)

- Kin Cheong Sou (Chalmers)
- Iman Shames (Univ. Melbourne)

- Julien M. Hendrickx (UC Louvain)
- Raphael M. Jungers (UC Louvain)

Course Outline

- Monday (8:30-10:30):
 - Lecture 1 (HS): Introduction, data attacks against non-dynamical systems, power network monitoring, security index, graph min cut
 - Tuesday (8:30-12:30):
 - Lecture 2 (HS): Attack space for cyber-physical systems: undetectable, stealth, covert, bias, DoS, replay attacks
 - Lecture 3 (AT): Defense mechanisms, risk management, anomaly detectors, watermarking
 - Wednesday (8:30-10:30):
 - Exercise session: **Hand in exercises before to get credits**
 - Lecture 4 (HS): Physical limits of control implementations
-

Key References for Lecture 1

- André Teixeira, Kin Cheong Sou, Henrik Sandberg, Karl Henrik Johansson: "Secure Control Systems: A Quantitative Risk Management Approach". IEEE Control Systems Magazine, 35:1, pp. 24-45, February 2015.
- Julien M. Hendrickx, Karl Henrik Johansson, Raphael M. Jungers, Henrik Sandberg, Kin Cheong Sou: "Efficient Computations of a Security Index for False Data Attacks in Power Networks". IEEE Transactions on Automatic Control: Special Issue on Control of Cyber-Physical Systems, 59:12, pp. 3194-3208, December 2014.

Lecture 1

- Background and motivation
- Adversaries in networked control systems
- Quantifying security: A case study in power system monitoring
- The security index, and its computation

ICS-CERT MONITOR



January – April 2014



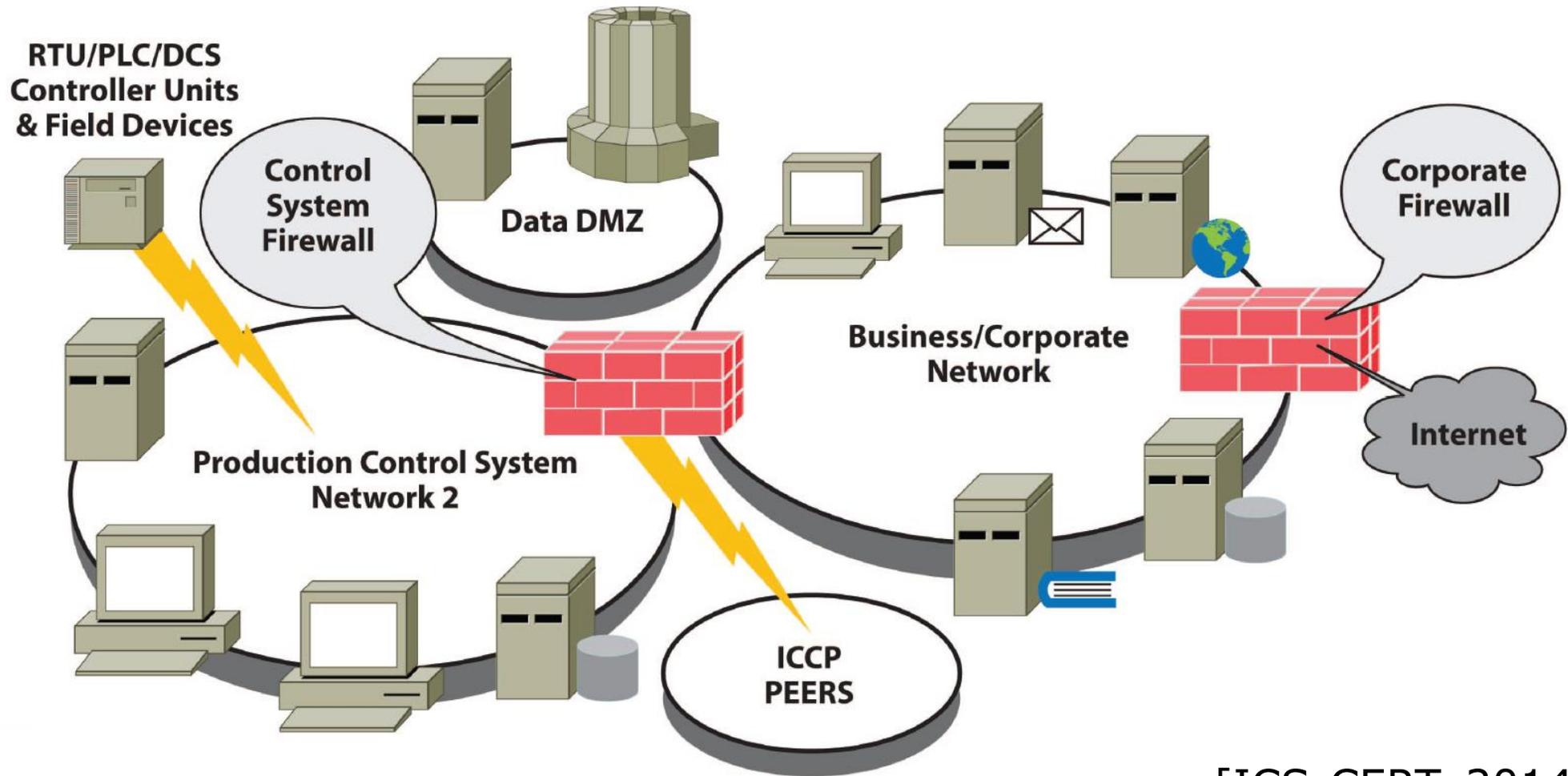
INCIDENT RESPONSE ACTIVITY

INTERNET ACCESSIBLE CONTROL SYSTEMS AT RISK

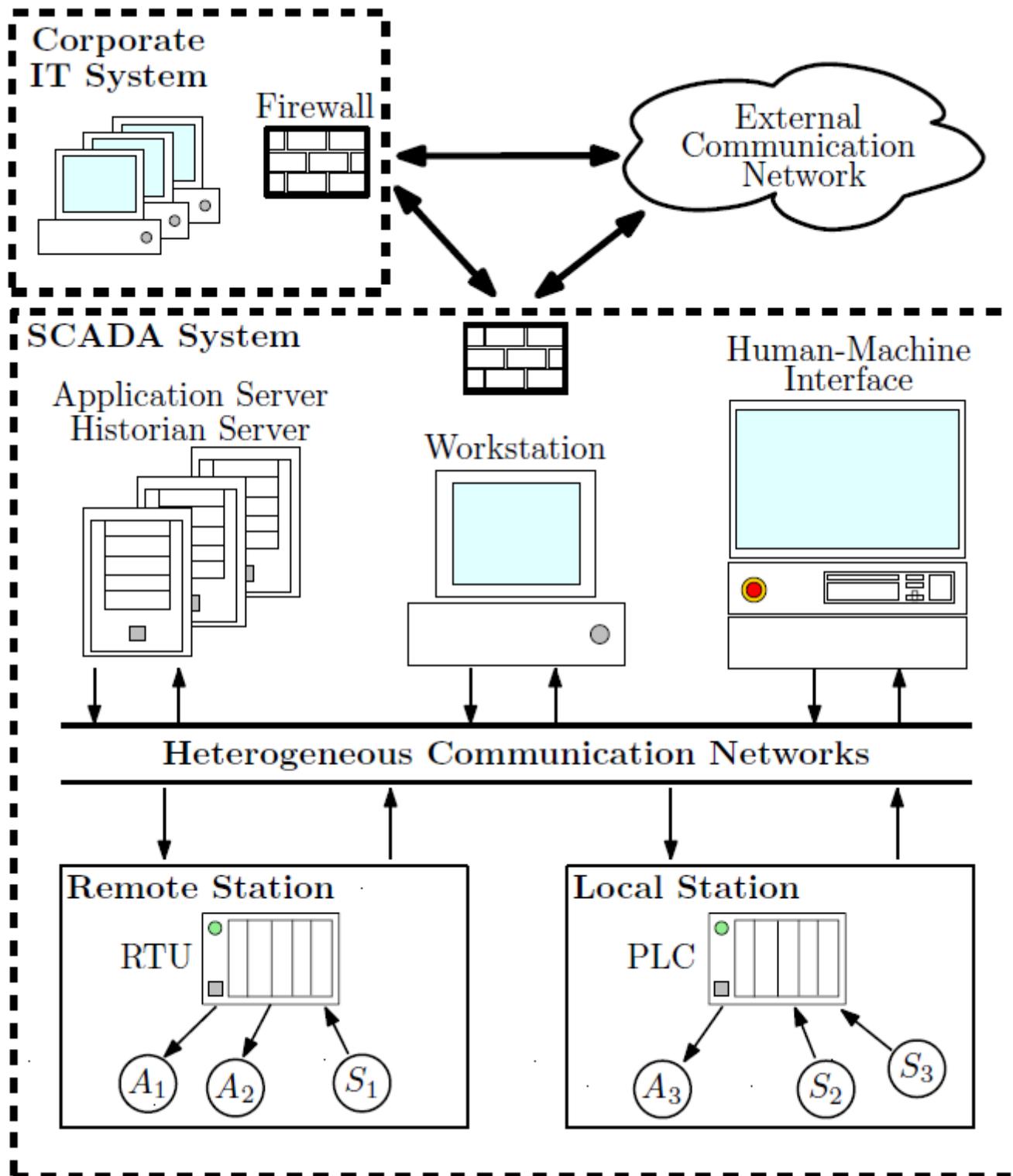
Is your control system accessible directly from the Internet? Do you use remote access features to log into your control system network? Are you unsure of the security measures that protect your remote access services? If your answer was yes to any or all these questions, you are at increased risk of cyber attacks including scanning, probes, brute force attempts and unauthorized access to your control environment.

ICS-CERT = Industrial Control Systems Cyber Emergency Response Team
(<https://ics-cert.us-cert.gov/>)
Part of US Department of Homeland Security

Example 1: Industrial Control System (ICS) Infrastructure



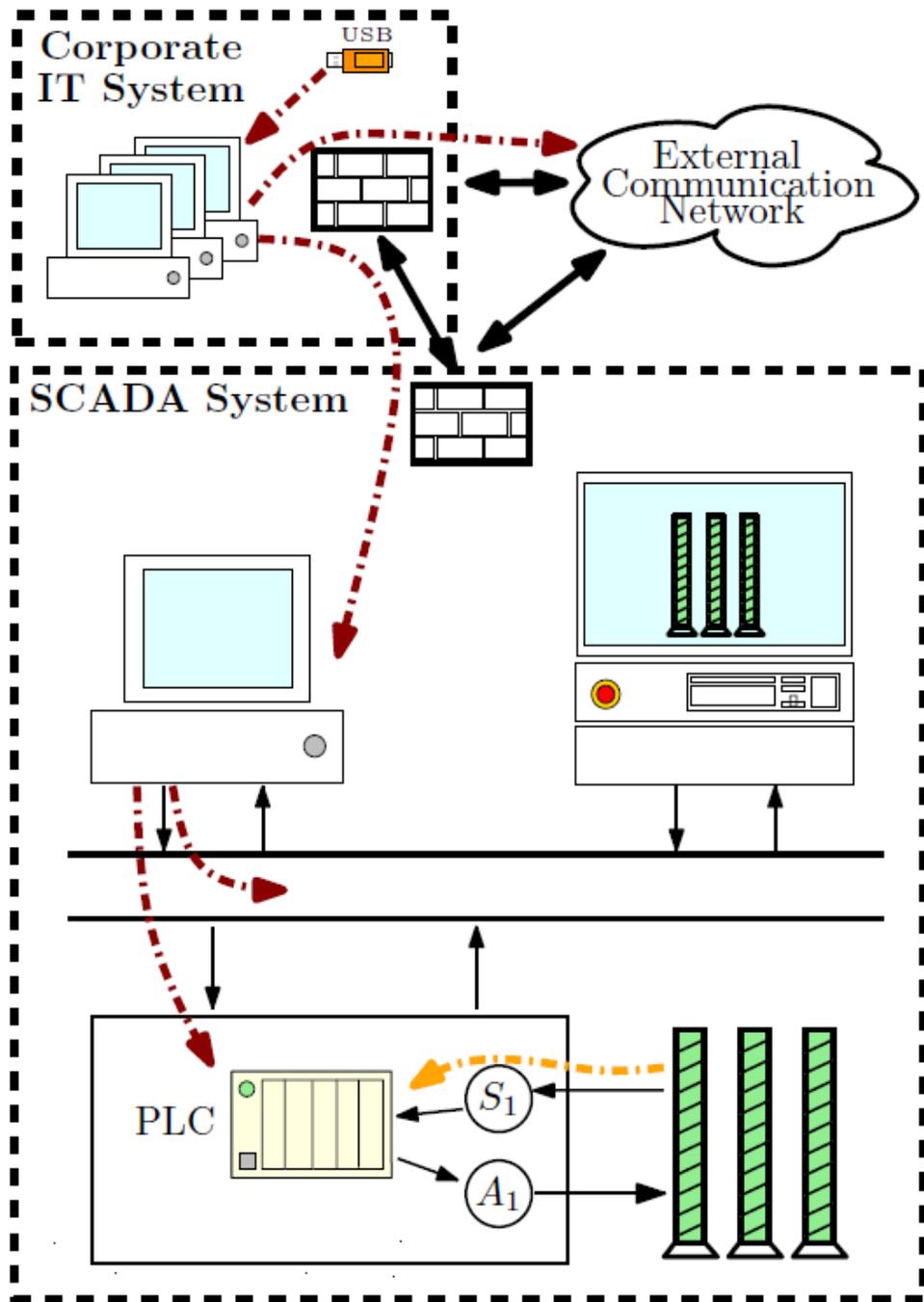
[ICS-CERT, 2014]



Example 2: The Stuxnet Worm (2010)

- **Targets:** Windows, ICS, and PLCs connected to variable-frequency drives
- Exploited **4 zero-day flaws**
- **Speculated goal:**
Harm centrifuges at uranium enrichment facility in Iran
- **Attack mode:**
 1. Delivery with USB stick (**no internet connection necessary**)
 2. Replay measurements to control center and execute harmful controls





(a) Infection and data recording.

Example 3: Attack Demo from SPARKS

- SPARKS: EU FP7 project
 - <https://project-sparks.eu/>
- A Multi-stage Cyber-attack Demonstration
 - <https://project-sparks.eu/publications/stakeholder-workshops/2nd-sparks-stakeholder-workshop/>

At the stakeholder workshop, a multi-stage cyber-attack demonstration was presented to the stakeholders. The aim of this demonstration was to highlight the nature of the cybersecurity problem for the smart grid. The attack demonstration implemented a number of steps, such as a social engineering attack, and exploited known software vulnerabilities to realise a man-in-the-middle attack between a IEC 61850 client and a photovoltaic inverter located at the [AIT smartEST lab](#) in Vienna, Austria.



SMART GRID PROTECTION AGAINST CYBER ATTACKS

Demonstration:
A Multi-Stage Cyber-attack to a Photovoltaic Inverter

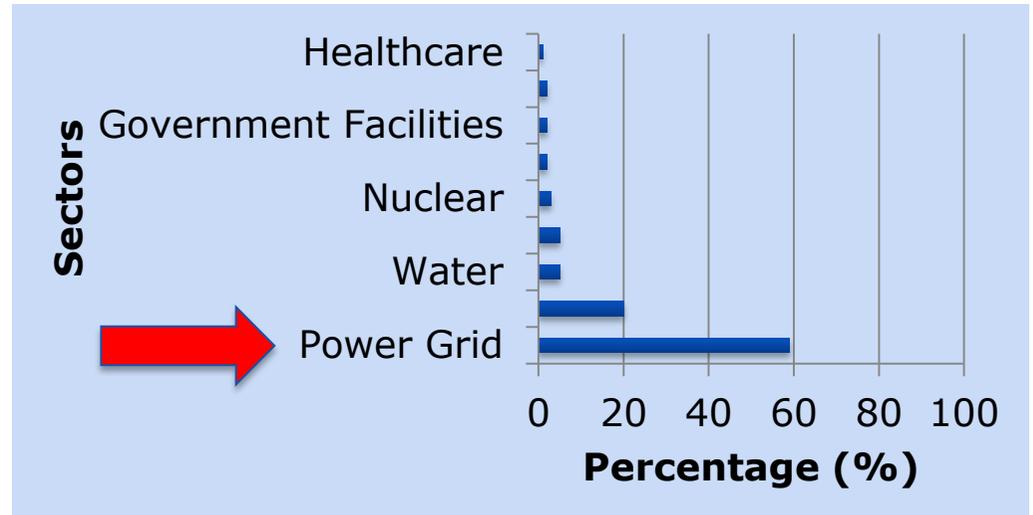
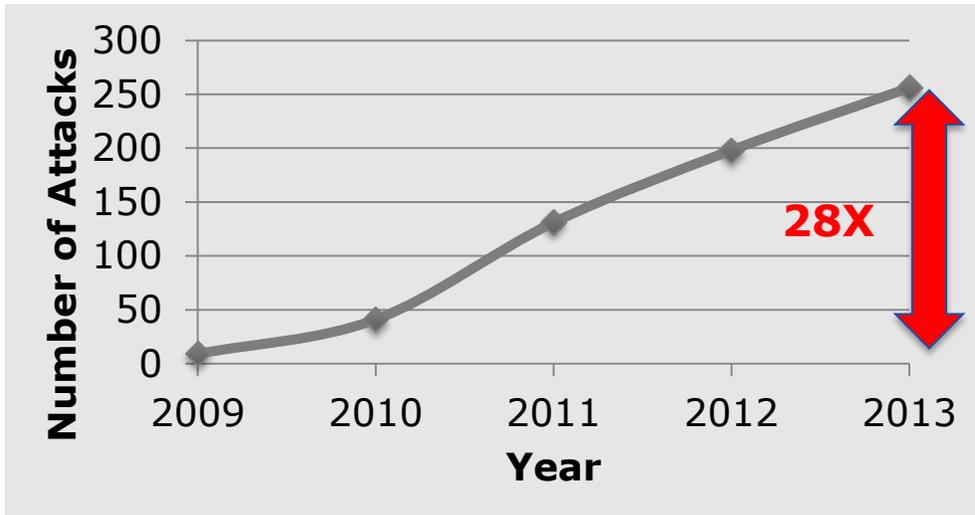
Dr Kieran McLaughlin, Dr BooJoong Kang
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Dr Silvio La Porta
EMC Corporation
Dr Friederich Kupzog, Dr Thomas Strasser
AIT Austrian Institute of Technology

Web: <https://project-sparks.eu>
Email: sparks-mgmt@ait.ac.at
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EU FP7 Programme Contract No. 608224 

Some Statistics

Cyber incidents in critical infrastructures in the US (Voluntarily reported to ICS-CERT)



[ICS-CERT, 2013]
[S. Zonouz, 2014]

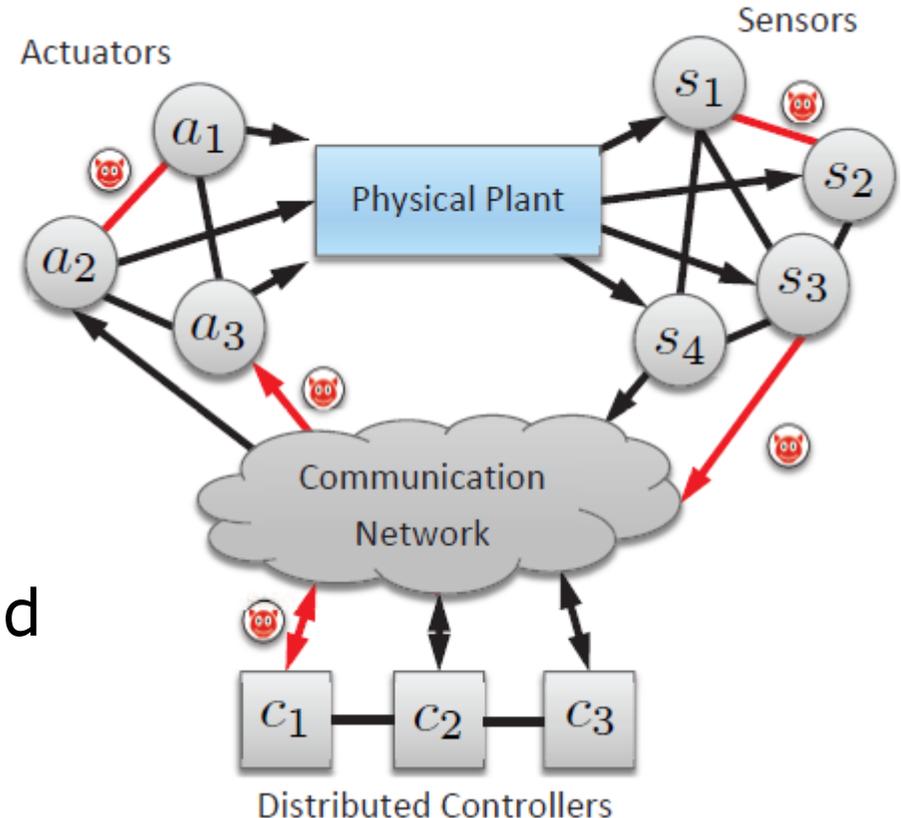
Cyber-Secure Control

Networked control systems

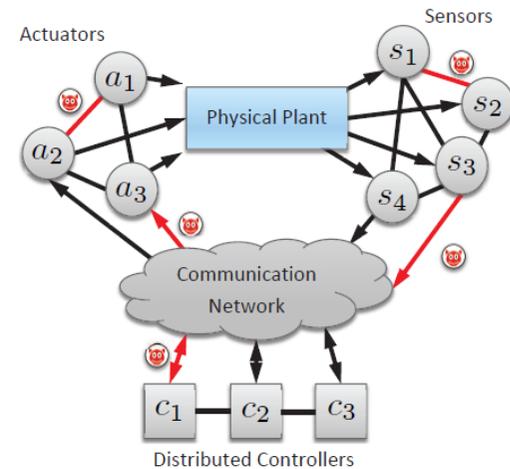
- are being **integrated with business/corporate networks**
- have many potential points of **cyber-physical attack**

Need tools and strategies to understand and mitigate attacks:

- Which threats should we care about?
- What impact can we expect from attacks?
- Which resources should we protect (more), and how?



Special Controls Perspective Needed?



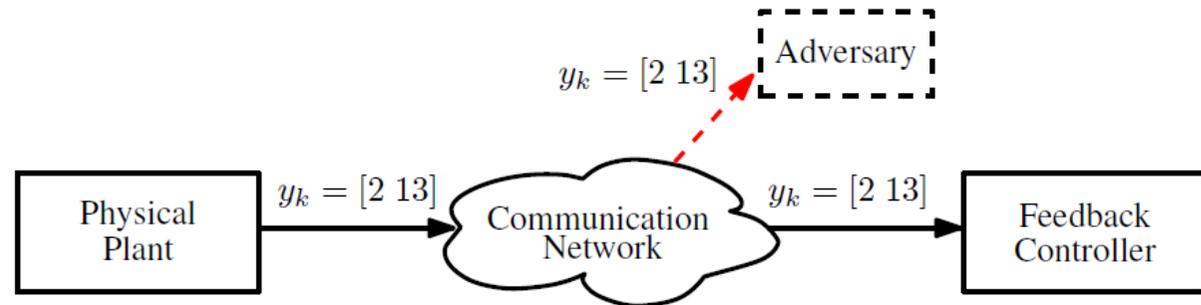
- Clearly IT security is needed: Authentication, encryption, firewalls, etc.

But not sufficient...

- Interaction between physical and cyber systems make control systems different from normal IT systems
- Malicious actions can enter anywhere in the closed loop and cause harm, whether channels secured or not
- Can we trust the interfaces and channels are really secured? (see OpenSSL Heartbleed bug...)

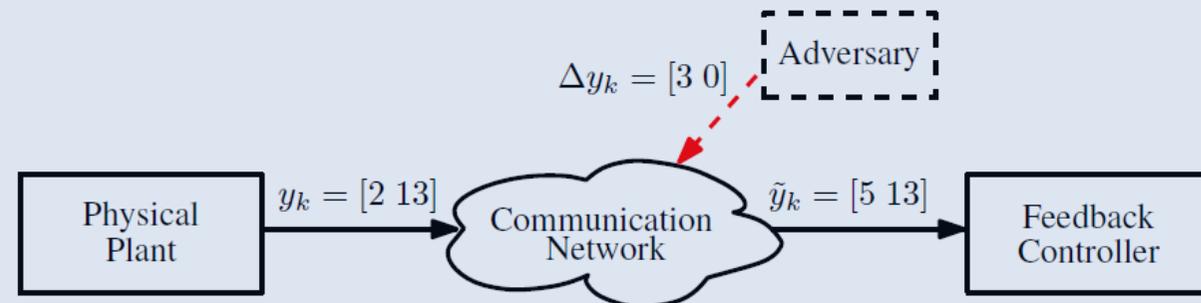
CIA in IT Security [Bishop, 2002]

- **C** – Confidentiality



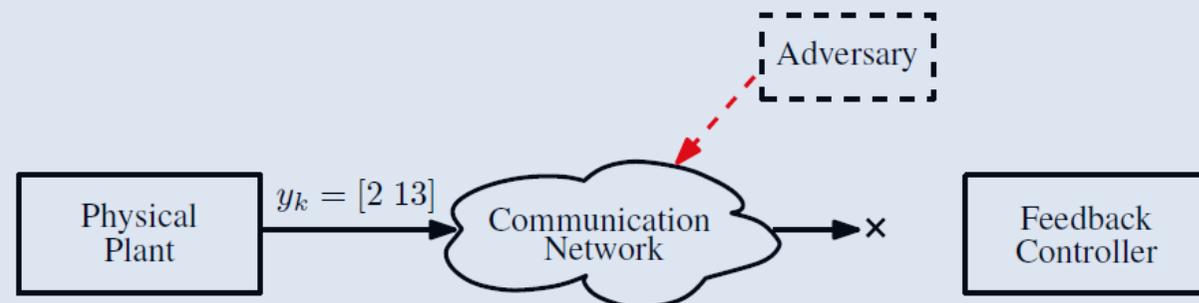
(a) Data confidentiality violation by a disclosure attack.

- **I** – Integrity



(b) Data integrity violation by a false-data injection attack.

- **A** – Availability



(c) Data availability violation by a denial-of-service attack.

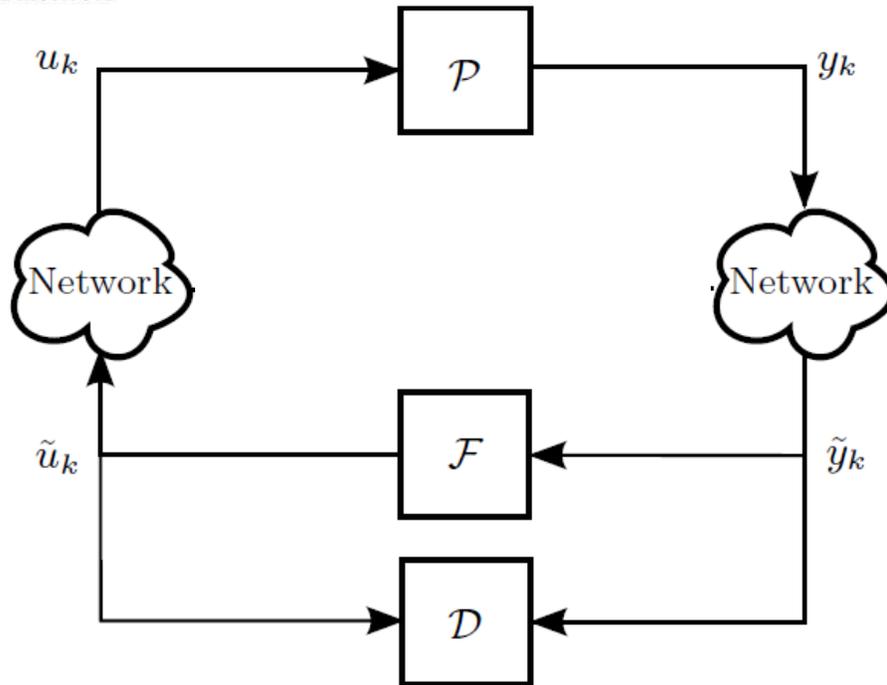
Practical Challenges and Opportunities

- Industrial Control Systems (ICSs) often a mix of old and new equipment. Improvements have to be **incremental**
- Many ICSs cannot easily be rebooted and patched with security updates
- How to best **collaborate** with **IT security** area?
Strive for “defense in depth”: Run several independent **security systems in parallel**

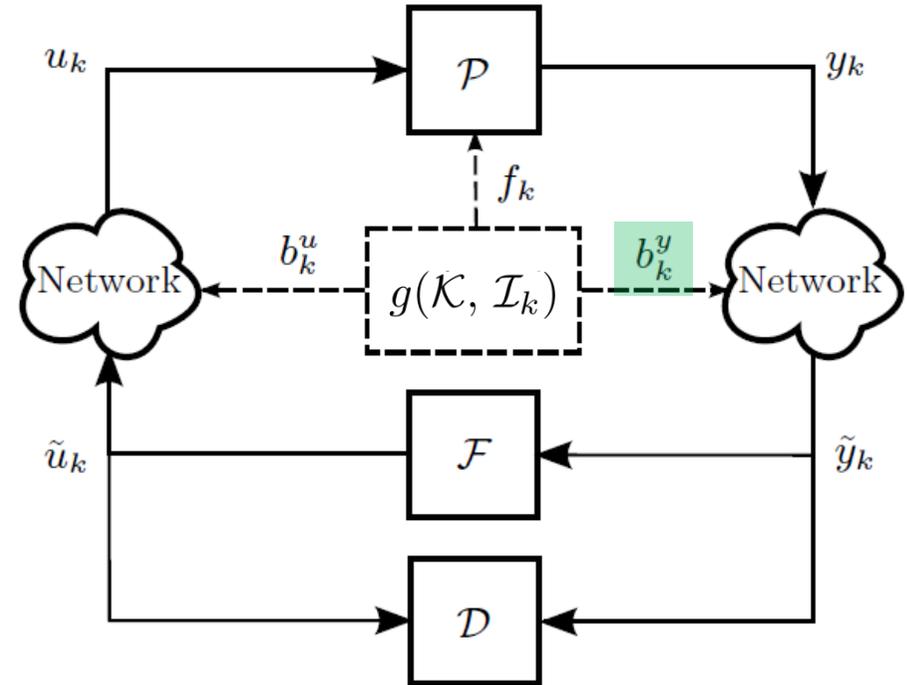
Lecture 1

- Background and motivation
- Adversaries in networked control systems
 - Which aspects are important to consider?
- Quantifying security: A case study in power system monitoring
- The security index, and its computation

Networked Control System under Attack



- Physical plant (\mathcal{P})
- Feedback controller (\mathcal{F})
- Anomaly detector (\mathcal{D})
- Disclosure Attacks



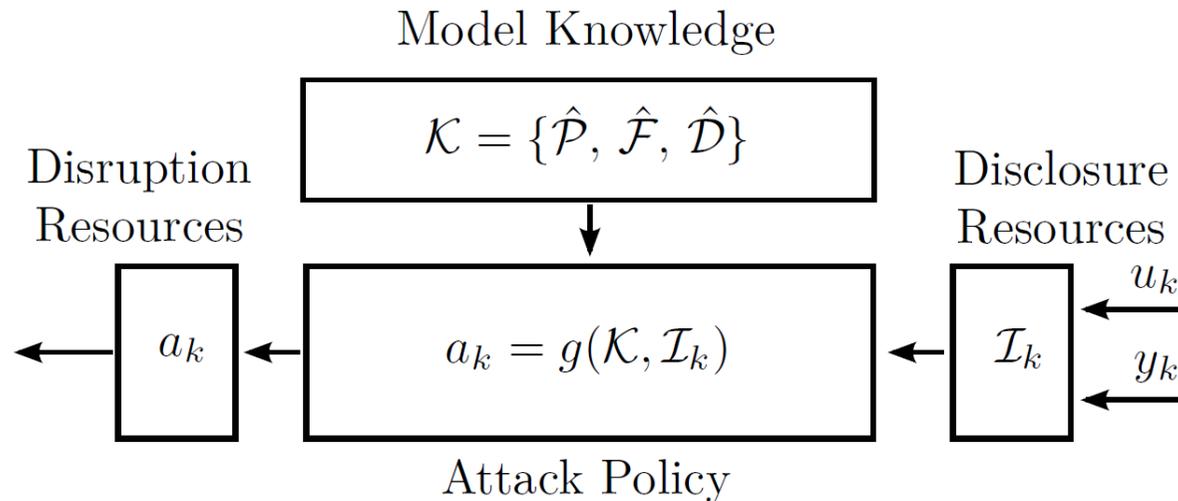
- Physical Attacks f_k
- Deception Attacks

$$\tilde{u}_k = u_k + \Gamma^u b_k^u$$

$$\tilde{y}_k = y_k + \Gamma^y b_k^y$$

Case study
later today

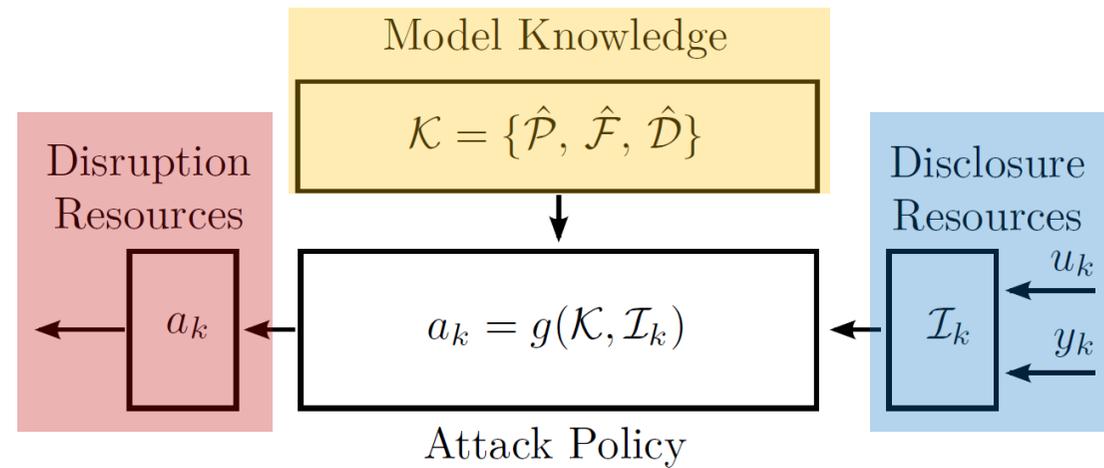
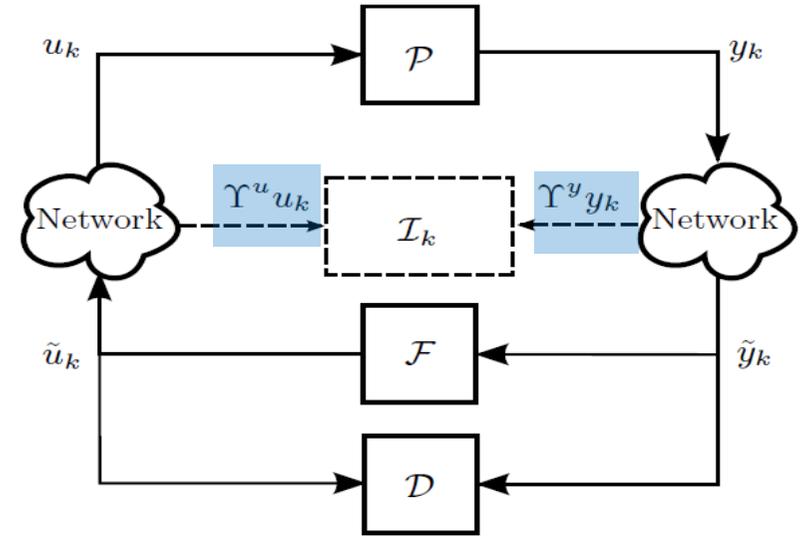
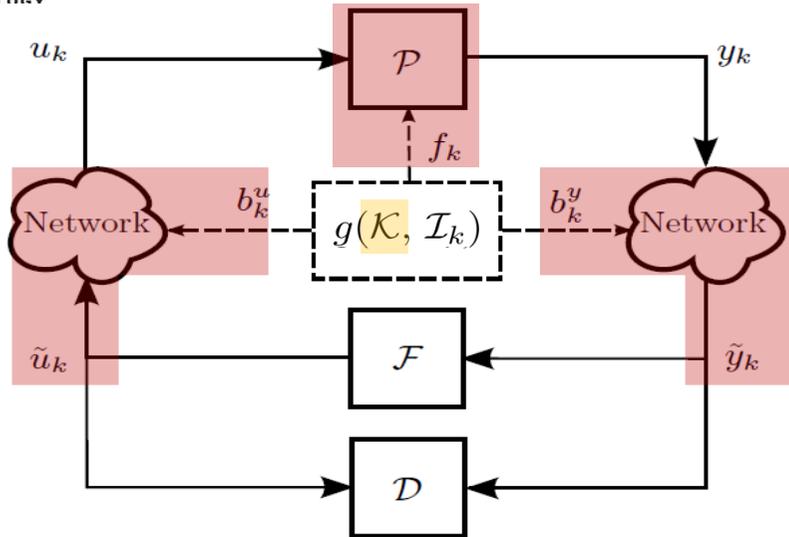
Adversary Model



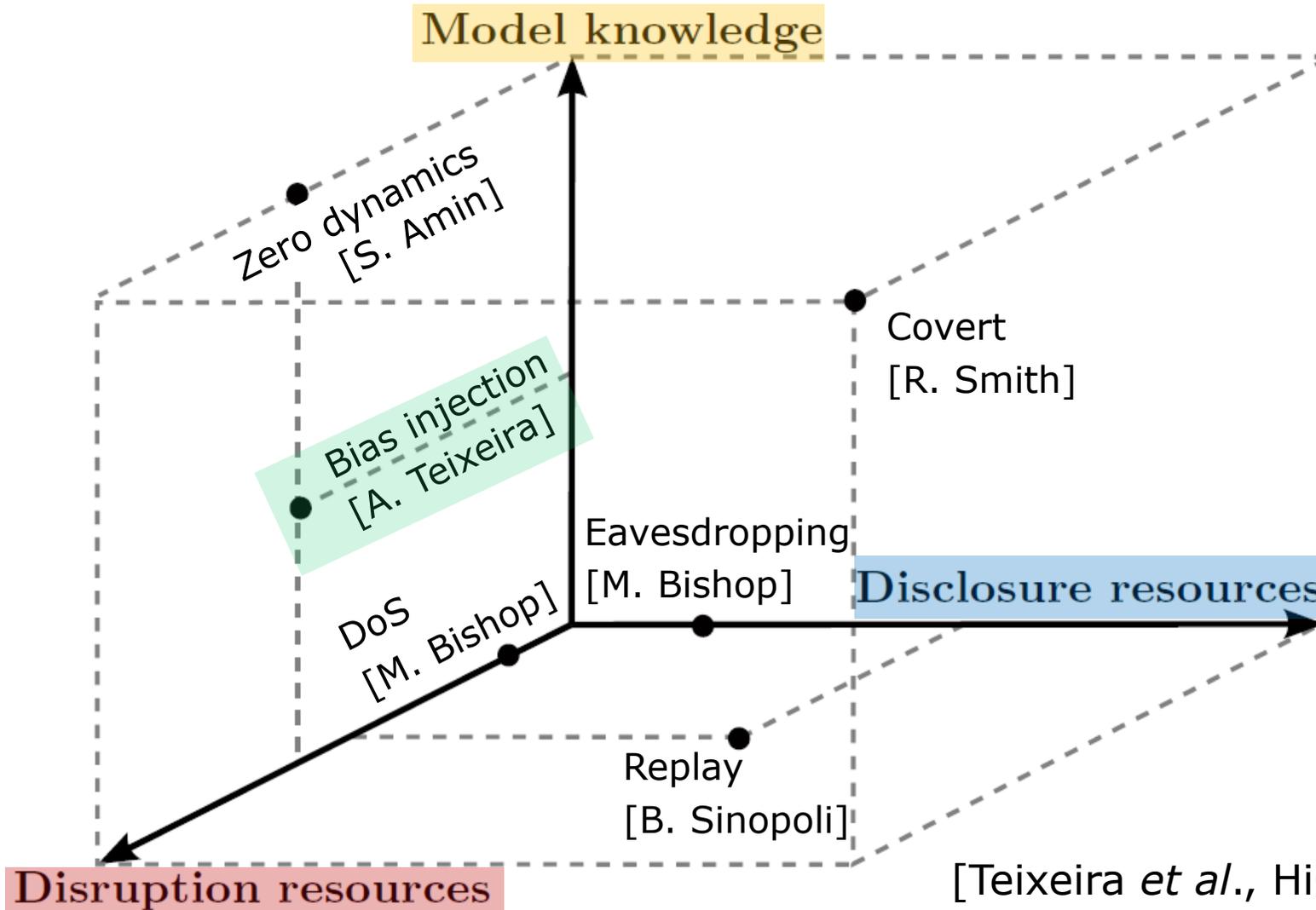
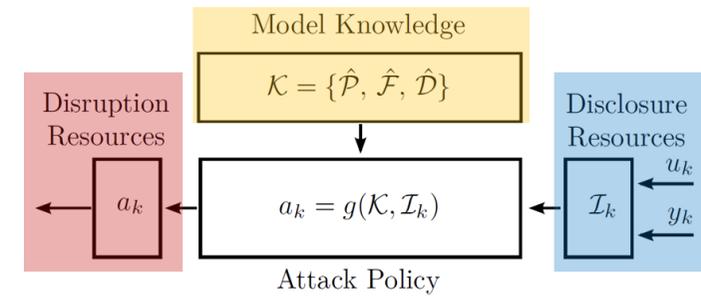
- **Attack policy:** Goal of the attack? Destroy equipment, increase costs,...
- **Model knowledge:** Adversary knows models of plant and controller? Possibility for stealthy attacks...
- **Disruption/disclosure resources:** Which channels can the adversary access?

[Teixeira *et al.*, HiCoNS, 2012]

Networked Control System with Adversary Model



Attack Space



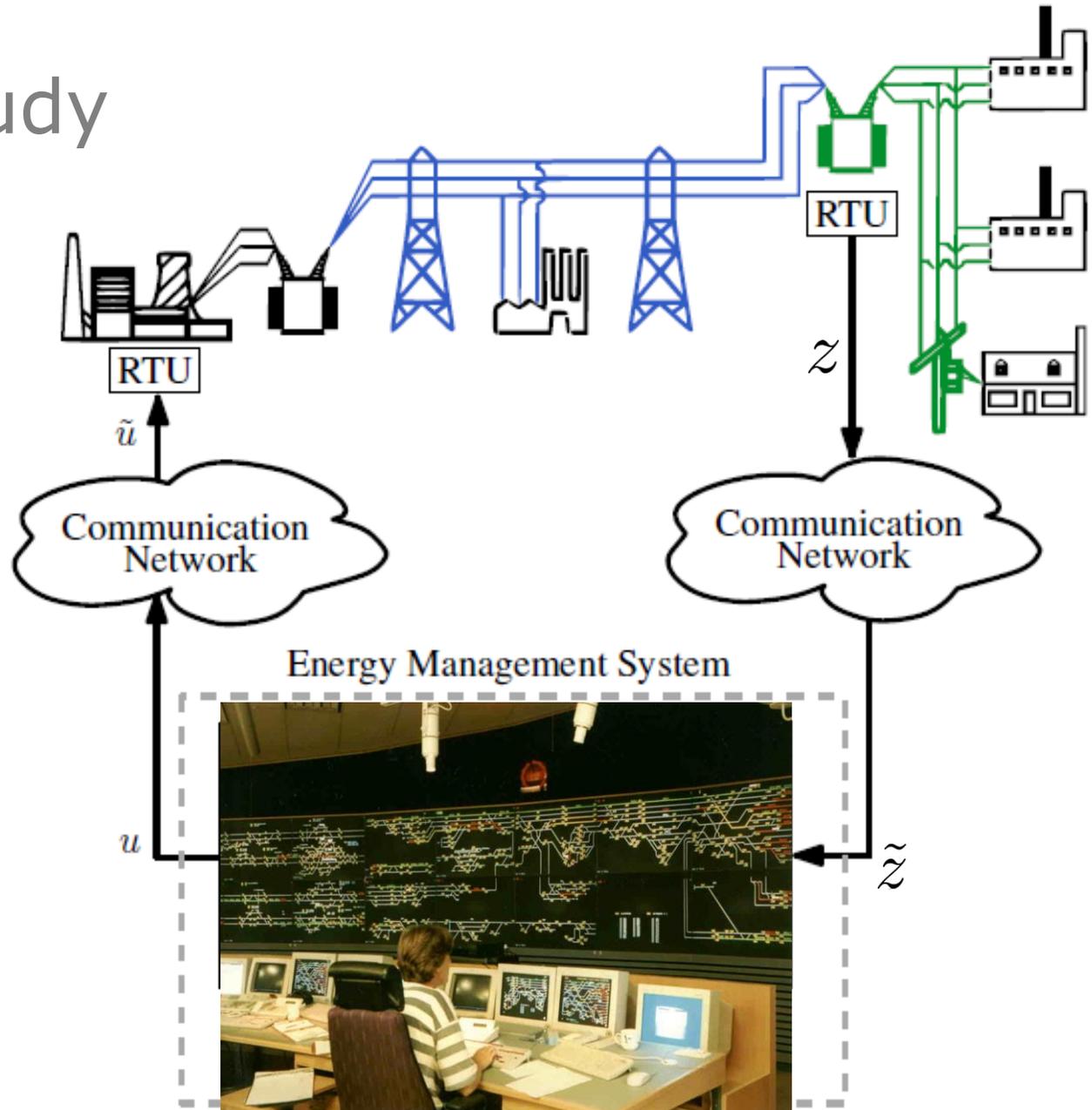
[Teixeira et al., HiCoNS, 2012]

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Case Study

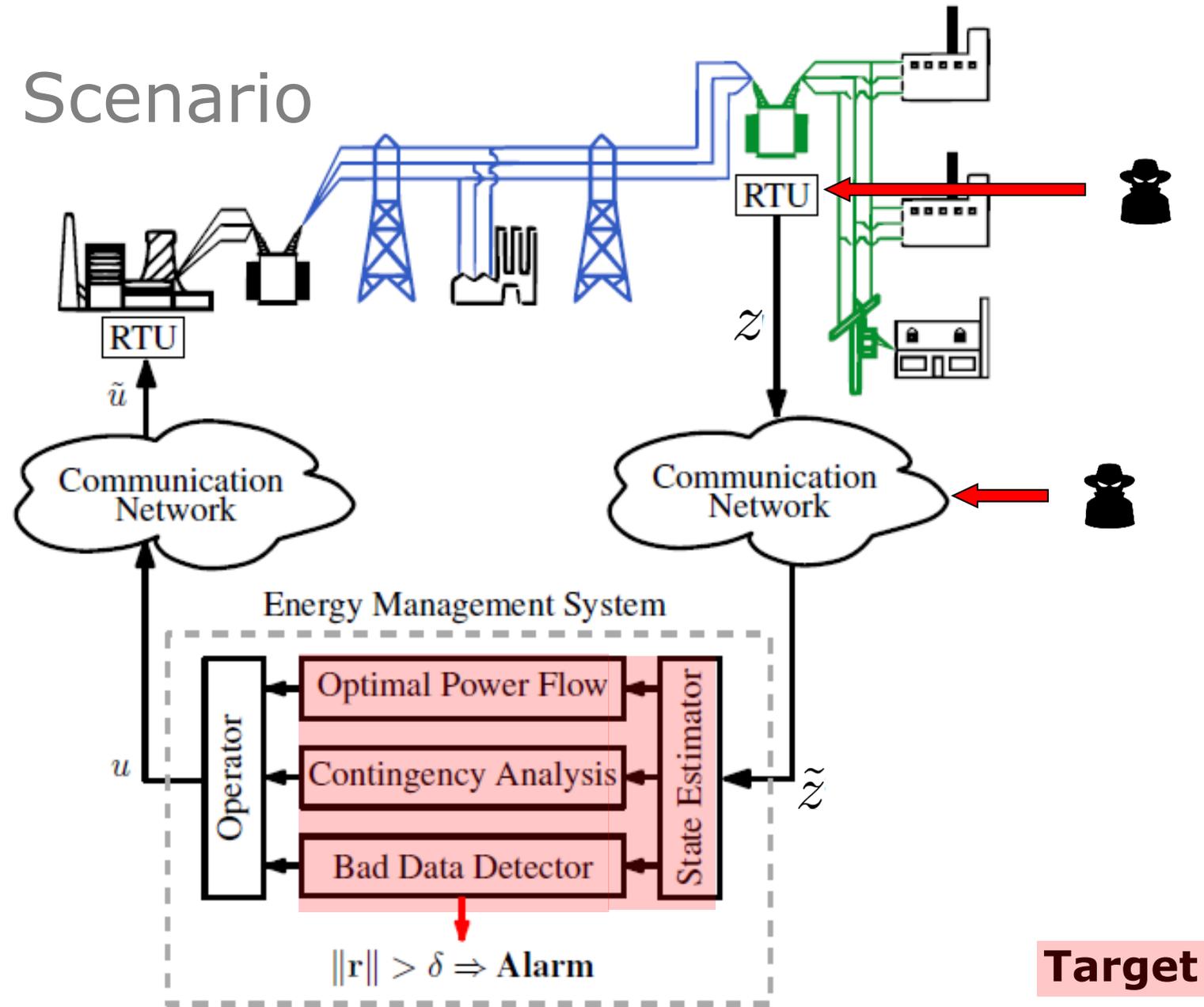
Transmission power system control and monitoring over networks



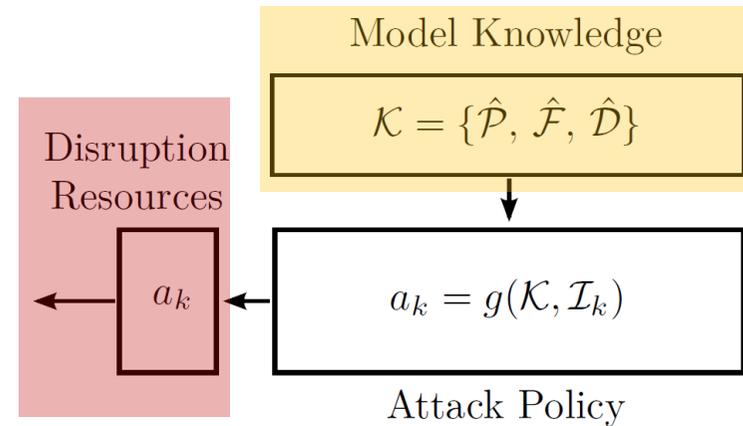
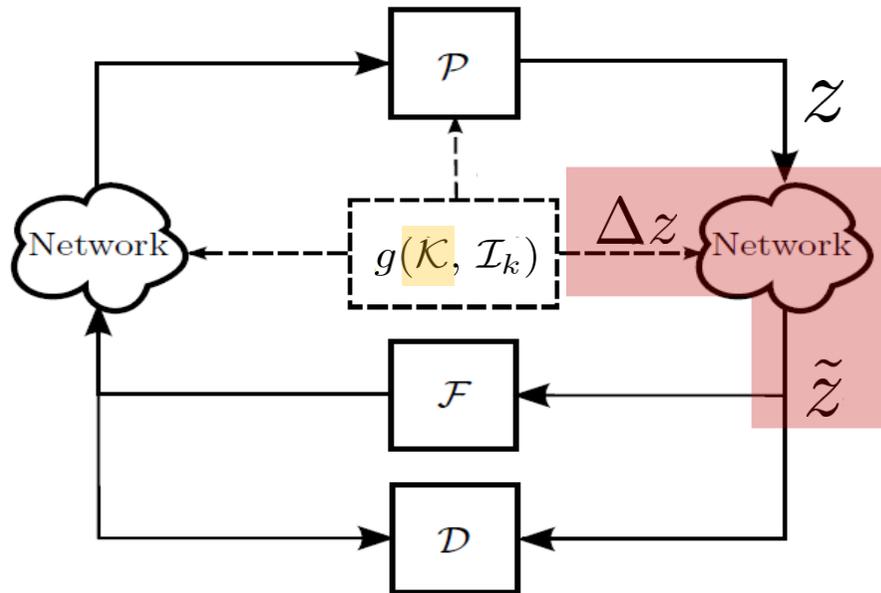
The Scenario

**Practically
motivated
problem...**

**How much
security does
the Bad Data
Detector
provide?**



Adversary Model



- **Attack policy:** Induce bias in power measurements without alarms
- **Model knowledge:** Steady-state model of power system
- **Disruption resources:** Small number of measurement channels

Can we quantify how hard such attacks would be?

Steady-State Power System Model

States (θ)
= bus voltage **phase angles**

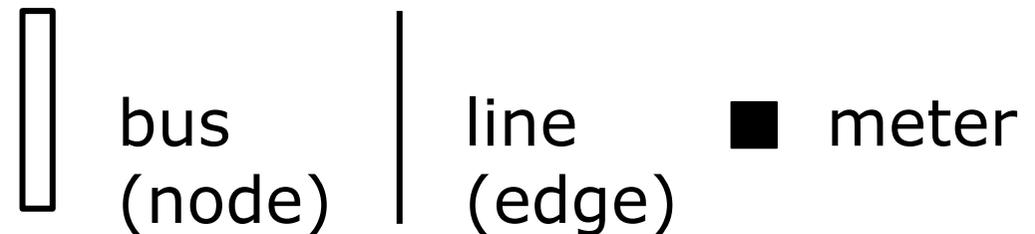
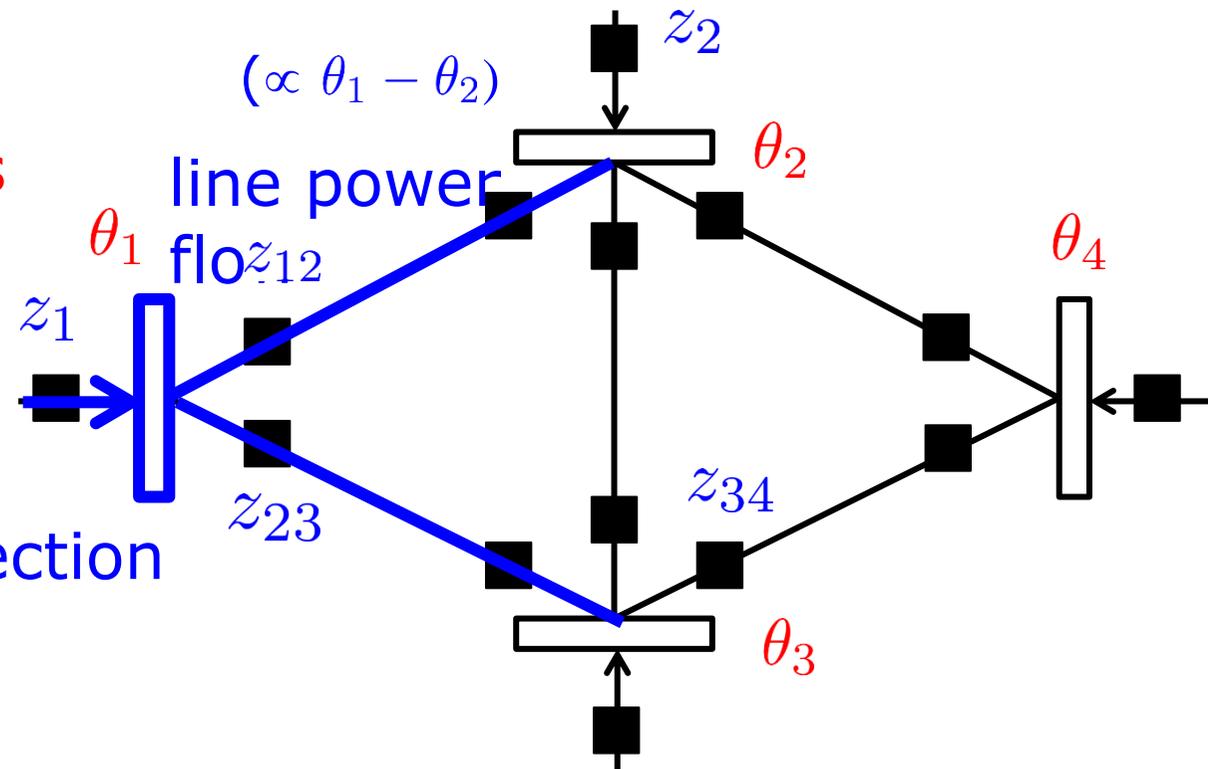
(flow conservation)
bus injection

Measurements (z)
= **line power flow & bus injection**

“DC power flow model”:

$$z = H\theta$$

← measurement matrix



Structure of Measurement Matrix H

$$H = \begin{bmatrix} P_1 D A^T \\ -P_2 D A^T \\ P_3 A D A^T \end{bmatrix} \begin{array}{l} \text{(flow measurements)} \\ \text{(flow measurements)} \\ \text{(injection measurements)} \end{array}$$

- A - directed incidence matrix of graph corresponding to power network topology
- D - nonsingular diagonal matrix containing reciprocals of reactance of transmission lines
- P - measurement selection matrices (rows of identity matrices)
- More measurements than states. Redundancy!



Example on the Board

State Estimation by Weighted Least Squares

State estimator (LS)

$$\tilde{z} = H_{2:} \theta_{2:} + \Delta z$$

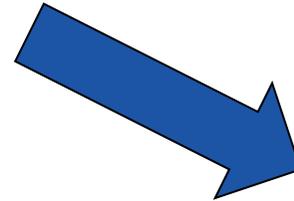
$$\Rightarrow \hat{\theta}_{2:} = (H_{2:}^T W H_{2:})^{-1} H_{2:}^T W \tilde{z}$$

wrong



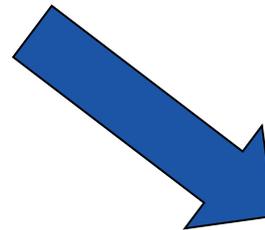
wrong

Contingency
analysis



wrong

OPF
calculations



•
•
•

What if the measurements were **wrong**?

$$\tilde{z} = z + \Delta z \quad \longrightarrow \quad \text{random measurement noise}$$

intentional data attack

$$\hat{\theta}_{2:} = \theta_{2:} + \Delta \theta_{2:}$$

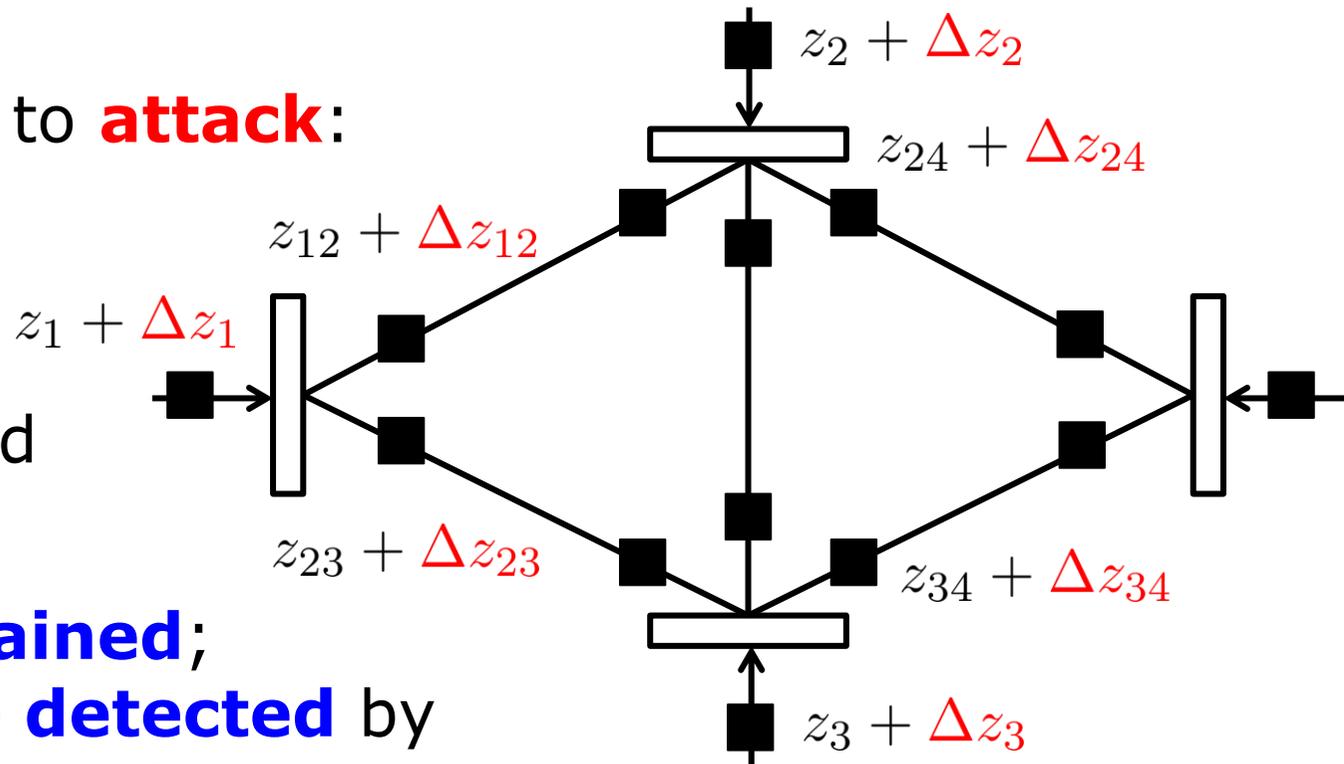
Stealthy Additive Deception Attack

Measurements subject to **attack**:

$$\tilde{z} = z + \Delta z$$

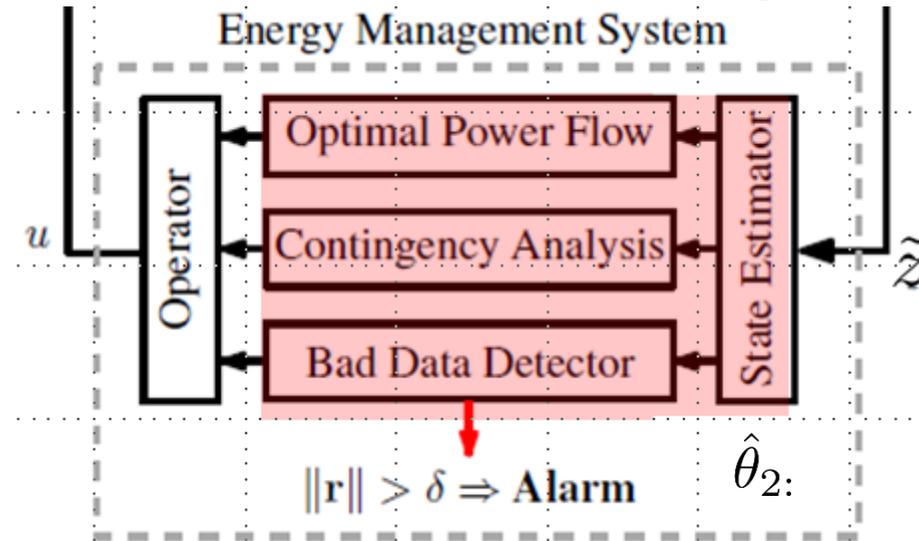
Is there a state explaining the received measurements?

Attack is **constrained**;
otherwise will be **detected** by
Bad Data Detection algorithm



Stealth attack: $\Delta z = H \Delta \theta$, arbitrary $\Delta \theta \in \mathbb{R}^{n+1}$

Bad Data Detection Algorithm



- $\mathbf{r} := \tilde{z} - H_2 \hat{\theta}_2$:

$$= (I - H_2 (H_2^T W H_2)^{-1} H_2^T W) \Delta z$$
- Stealth attack: $\Delta z = H \Delta \theta$, arbitrary $\Delta \theta \in \mathbb{R}^{n+1}$
- $\mathbf{r} \equiv 0$, since $H \Delta \theta = H_2 \Delta \theta_2$ for some $\Delta \theta_2 \in \mathbb{R}^n$

Quantification: Security Index

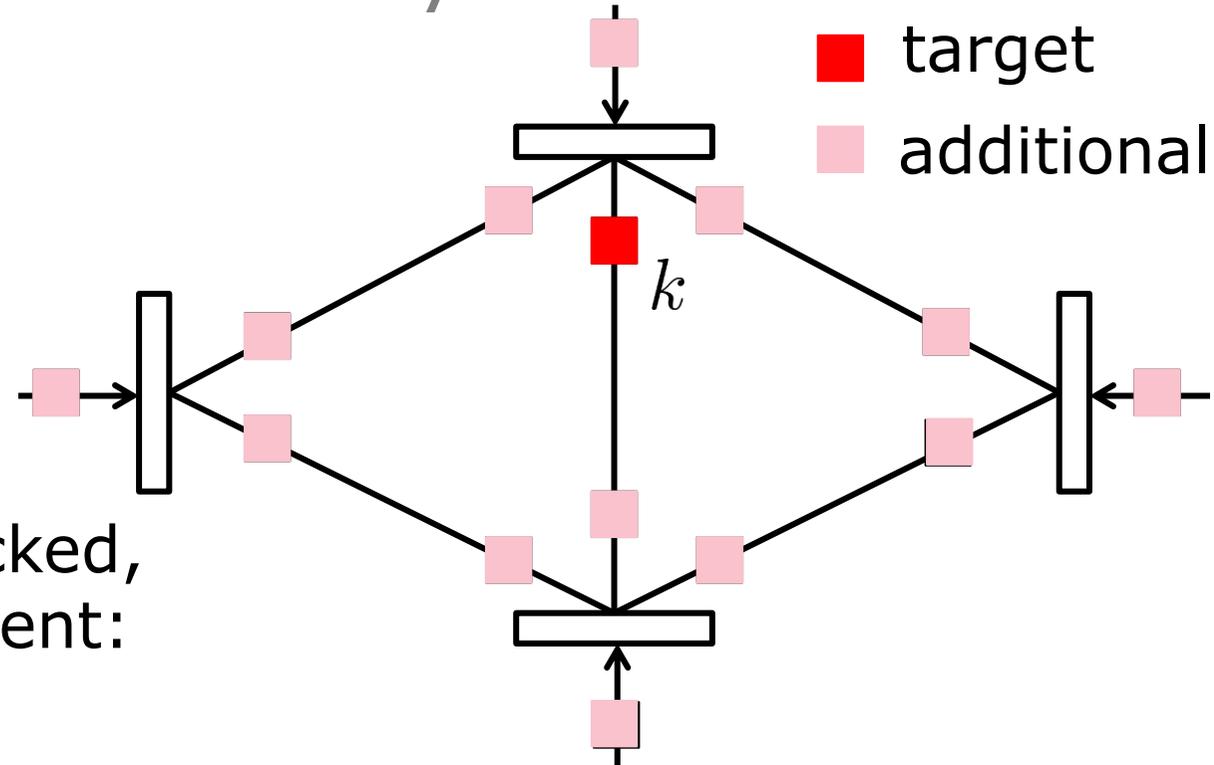
Stealth attack $\Delta z = H \Delta \theta$

In general, $e_k \notin \text{span}(H)$

Minimum # of meters attacked,
targeting the k^{th} measurement:

$$\min_{\Delta \theta \in \mathbb{R}^{n+1}} \text{card}(H \Delta \theta)$$

$$\text{s.t. } H(k, :) \Delta \theta = 1$$

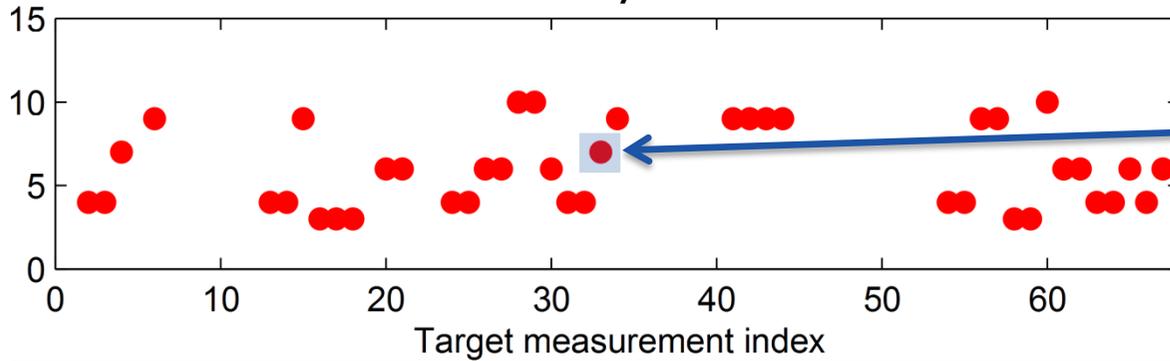


Minimum objective value =
security index

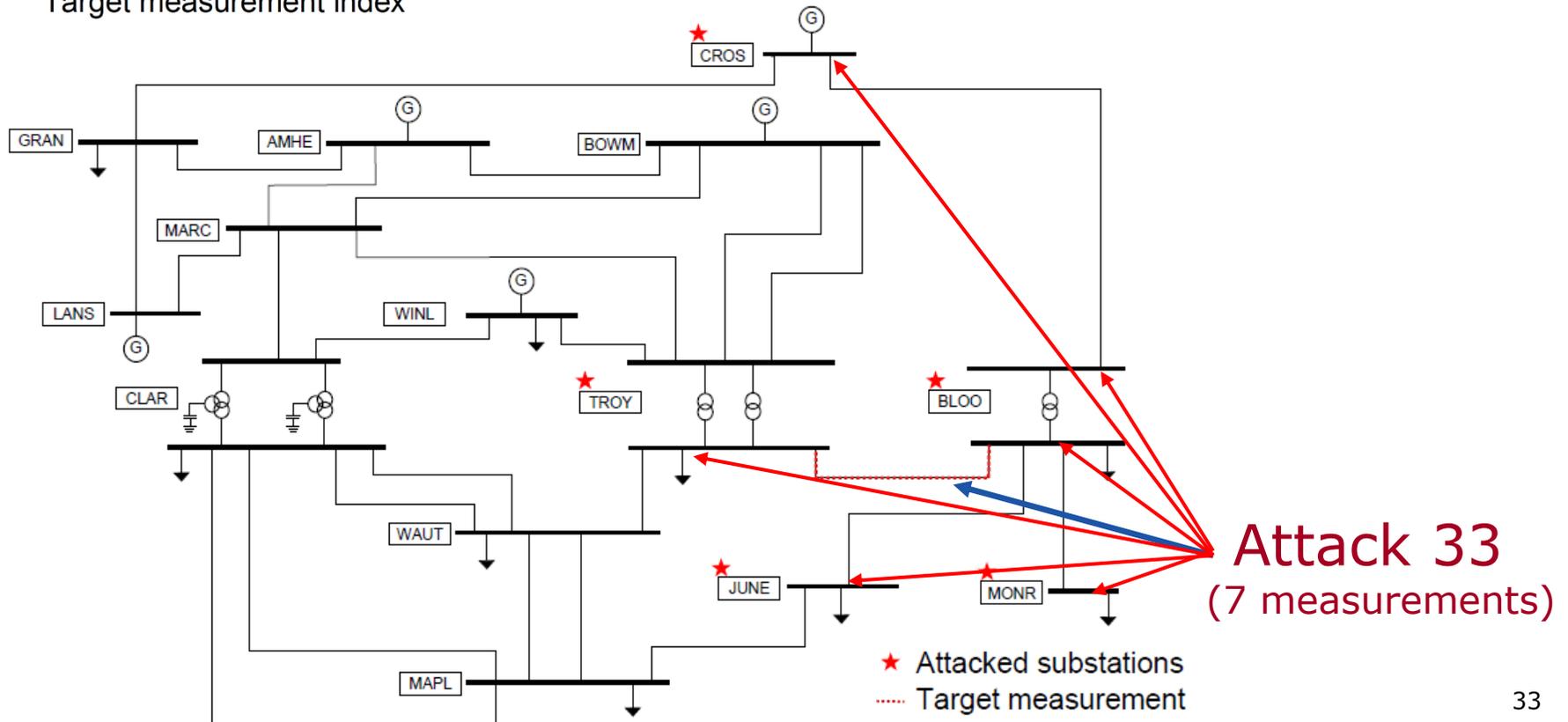
[Sandberg *et al.*, CPSWEEK, 2010]

Security Indices for 40-bus Network

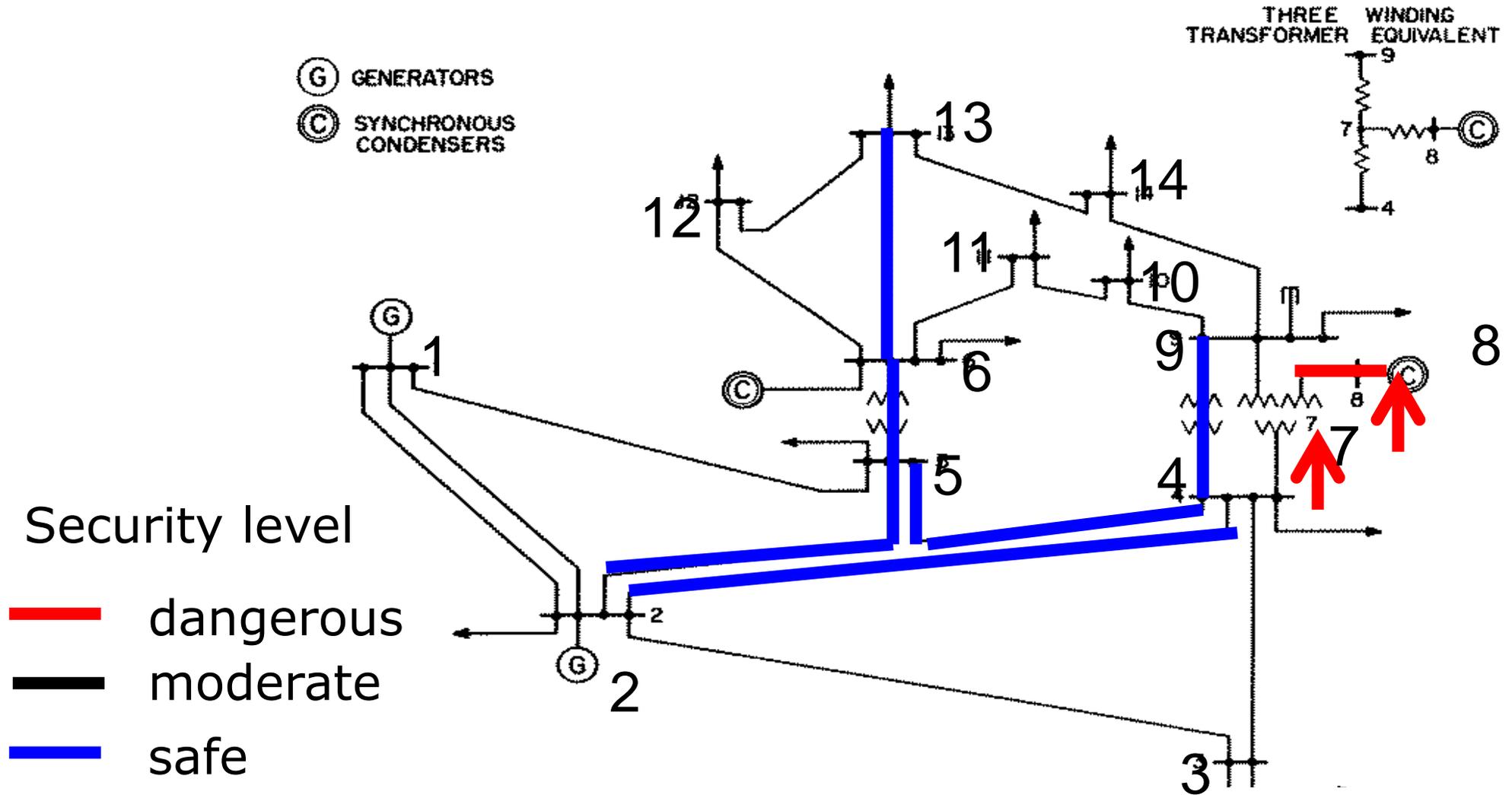
security index



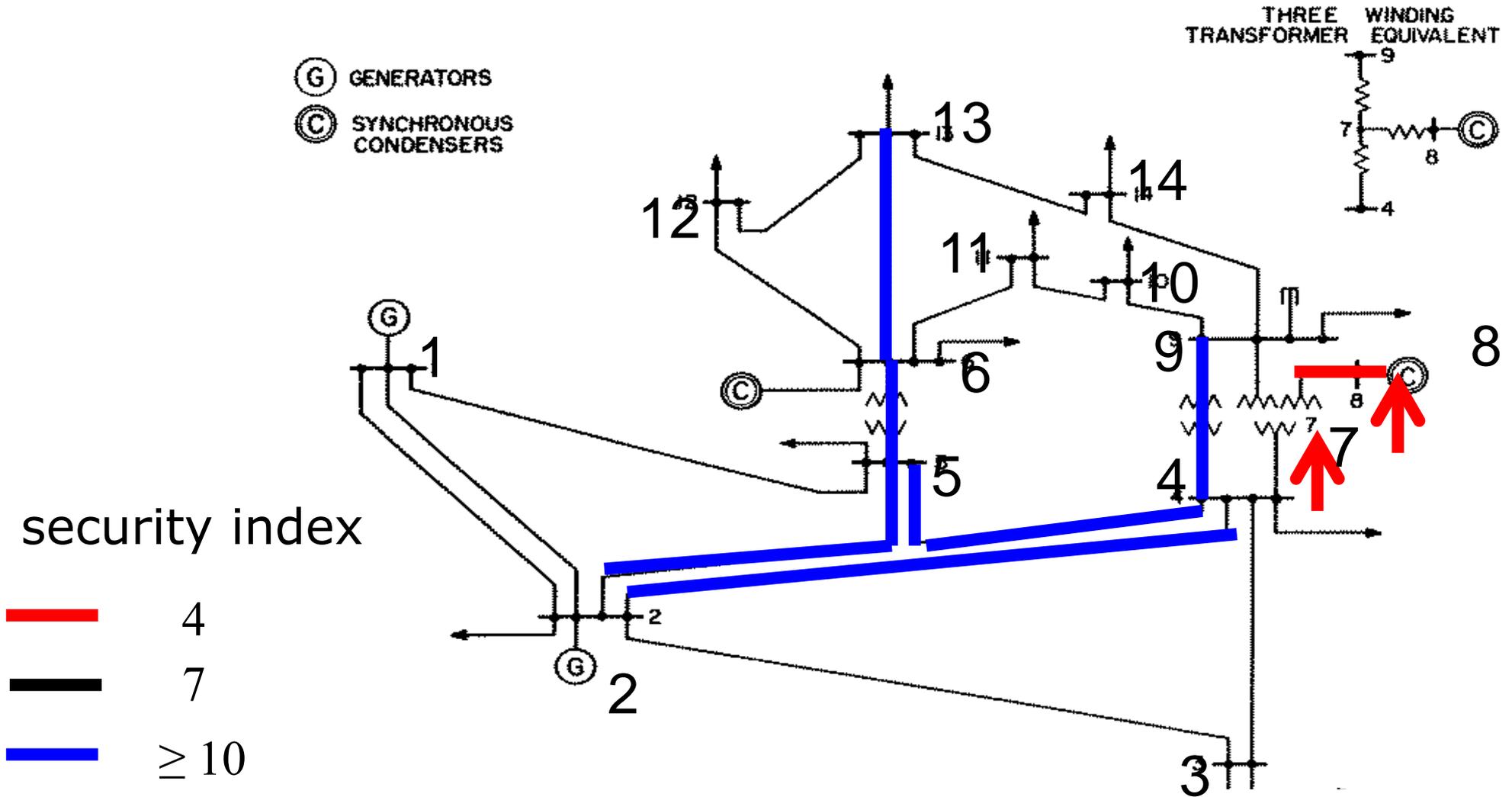
At least 7 measurements involved in a stealth attack against measurement 33



The Goal: Quantify Security to Aid Allocation of Protection



IEEE 14 Bus Vulnerable Measurements



Security index problem

$$\min_{\Delta\theta \in \mathbb{R}^{n+1}} \text{card}(H\Delta\theta)$$

$$\text{s.t. } H(k, :) \Delta\theta = 1$$

How to solve?

Closely related to compressed sensing and computation of **cospark** of H [Tillmann and Pfetsch, IEEE TIT, 2013].

Problem known to be **NP-hard** for arbitrary H .

[Theorem 1, Hendrickx *et al.*, IEEE TAC, 2014]

Security Index Computation – MILP

$$\begin{aligned} \min_{\Delta\theta \in \mathbb{R}^{n+1}} \quad & \text{card}(H\Delta\theta) \\ \text{s.t.} \quad & H(k, :) \Delta\theta = 1 \end{aligned}$$

- ❑ Cardinality minimization problem
- ❑ Mixed integer linear program (MILP)
- ❑ Big M reformulation
- ❑ **Exact** solution (solver: CPLEX)
- ❑ Solution algorithm **not scalable**

$$\min_{\Delta\theta, z} \sum_i z(i)$$

s.t.

$$-Mz \leq H\Delta\theta \leq Mz$$

$$H(k, :) \Delta\theta = 1$$

$$z(i) \in \{0, 1\} \quad \forall i$$

MILP formulation

(Exercise 1)

Security Index Computation – LASSO

$$\min_{\Delta\theta} \|H\Delta\theta\|_1$$

s.t. $H(k, :)\Delta\theta = 1$

- ❑ Convex linear program (LP)
- ❑ Known as LASSO
- ❑ **Approximate** solution
- ❑ Less expensive to solve

$$\min_{\Delta\theta, z} \sum_i z(i)$$

s.t.

$$-z \leq H\Delta\theta \leq z$$

$$H(k, :)\Delta\theta = 1$$

$$z(i) \in \mathbb{R} \quad \forall i$$

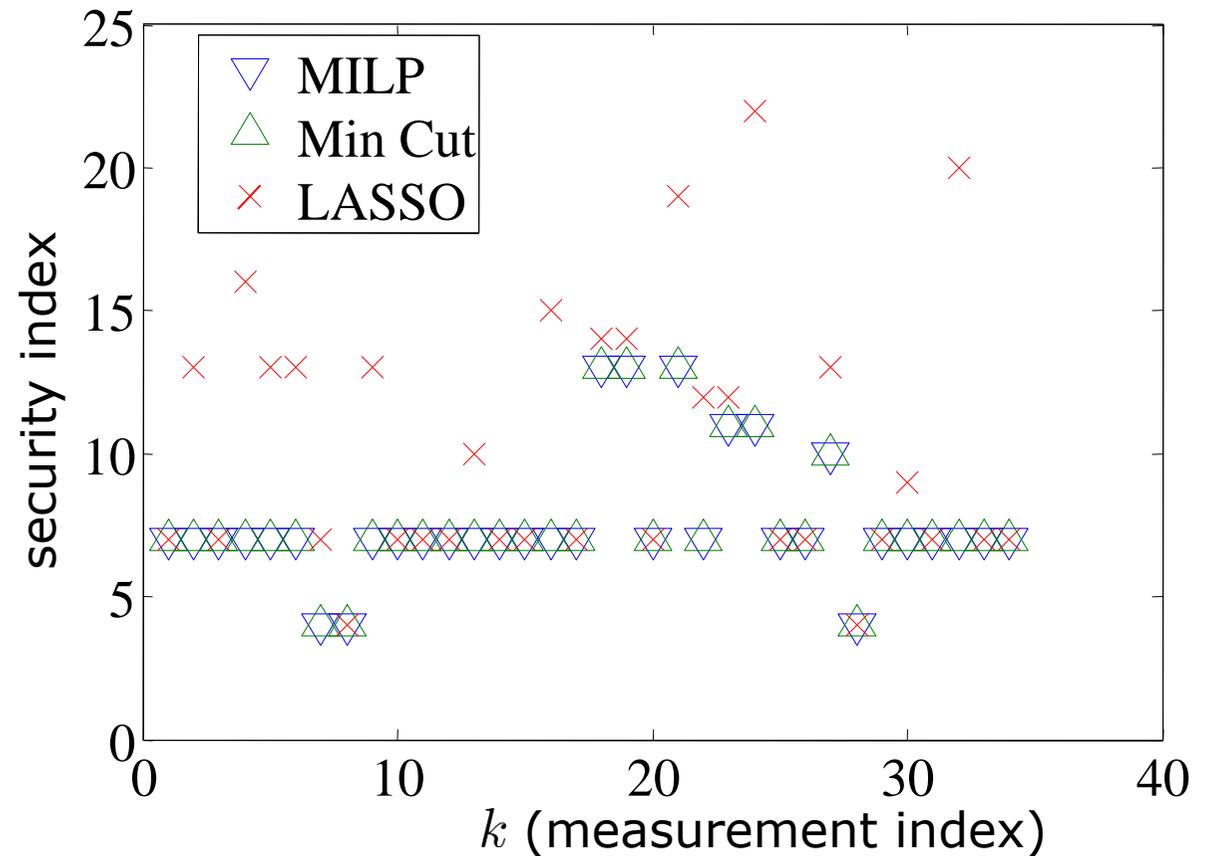
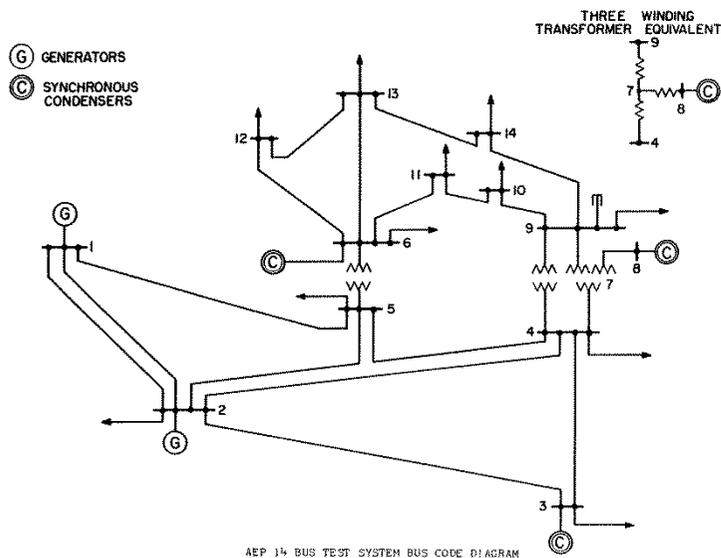
LP formulation

Wish List

- Can we find solutions as **accurately** as MILP, and **faster** than LASSO?
 - Arbitrary H : **No!** (Problem NP-hard)
 - H with the special physical and measurement structure: **Yes!** (**Min Cut** polynomial time algorithm next)
- Can we find methods giving more **problem insight**, and ideas for **assigning protection**?
 - **Yes**, exploit graph interpretation of solution

IEEE 14 Bus Benchmark Test Result

Security indices for all measurements



Solve time: MILP 1.1s; LASSO 0.6s; Min Cut 0.02s

IEEE 118, 300, 2383 Bus Benchmarks

Min Cut solution is **exact**

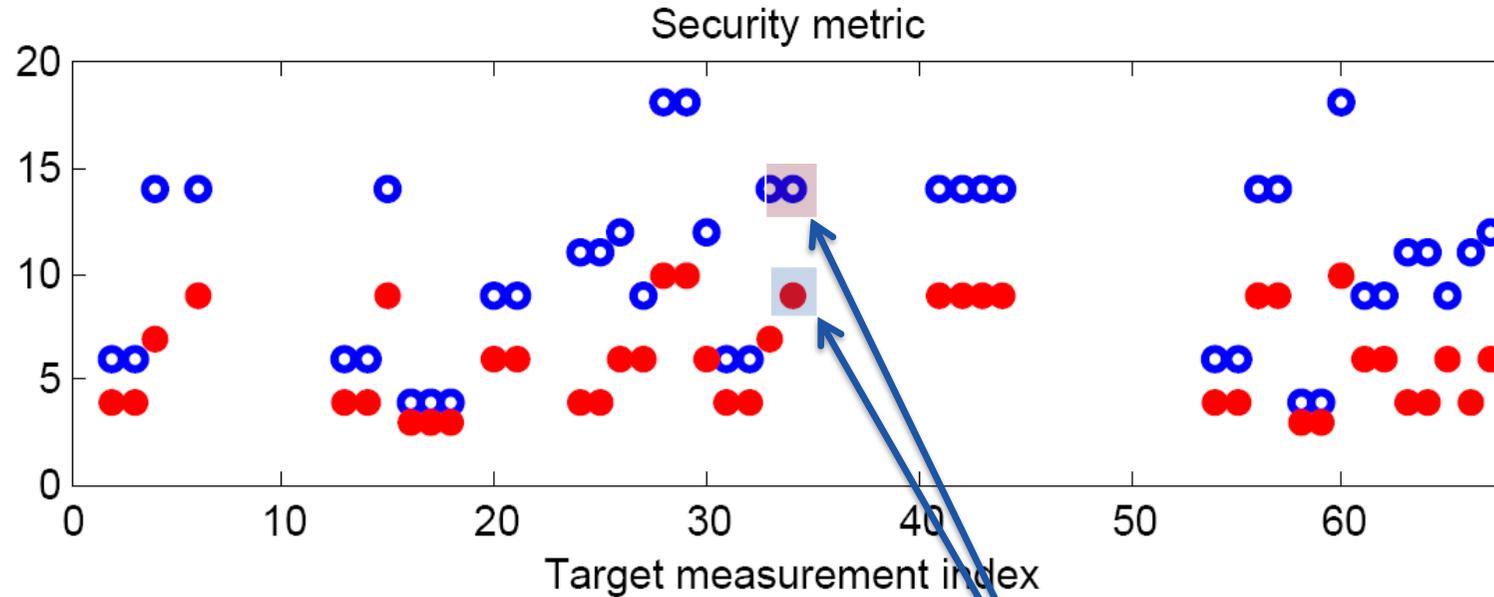
Solve time comparison:

Method/Case	118 bus	300 bus	2383 bus
MILP	763 sec	6708 sec	About 5.7 days
Min Cut	0.3 sec	1 sec	31 sec

Wish List

- Can we find solutions as **accurately** as MILP, and **faster** than LASSO?
 - Arbitrary H : **No!** (Problem NP-hard)
 - H with the special physical and measurement structure: **Yes!** (Min cut polynomial time algorithm next.)
- Can we find methods giving more **problem insight**, and ideas for **assigning protection**?
 - **Yes**, exploit graph interpretation of solution
 - **Securing sensors that are frequently cut gives indirect protection to many sensors!**
[Vukovic *et al.*, JSAC, 2012]

Assigning Protection Using Insight from Min Cut



- = Current measurement config.
- = Upgraded measurement config.

With only a few sensors protected, 14 instead of 7 measurements has to be involved in a stealth attack!

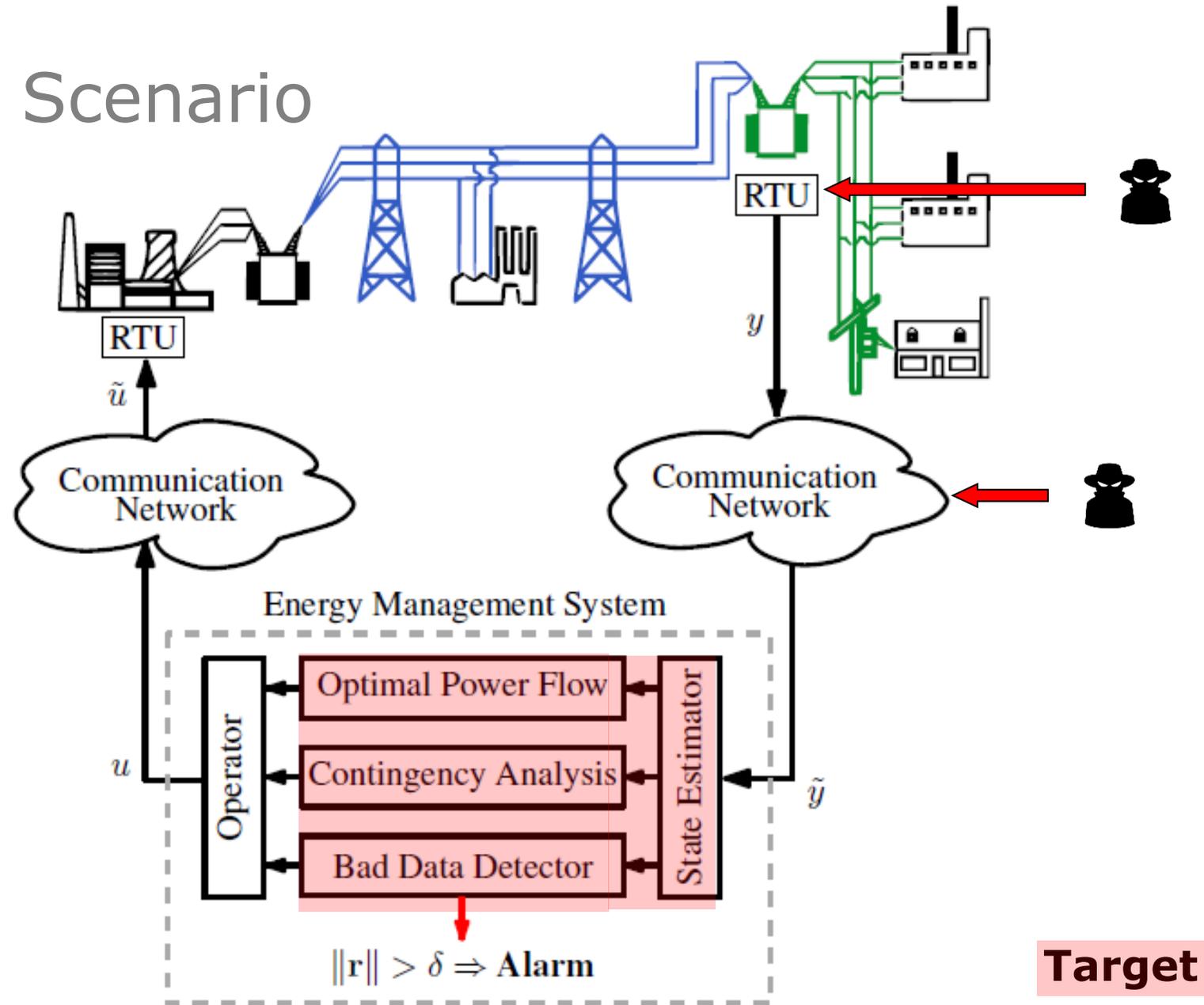
(Exercise 2)

The Scenario

Practically motivated problem...

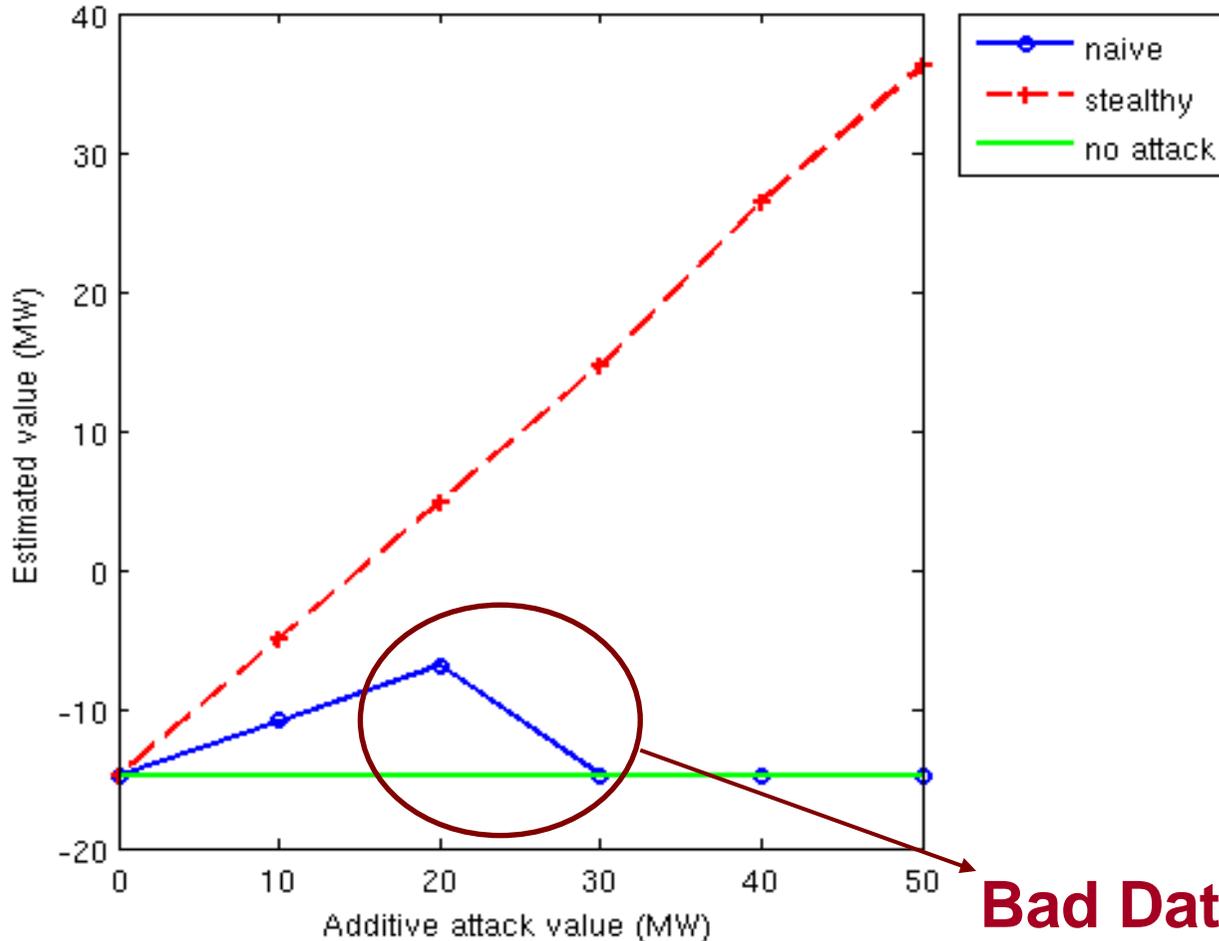
How much security does the Bad Data Detector provide?

Some, when security index is high



Verification in SCADA Testbed

Attacks on measurement 33



False value (MW)	Estimated value (MW)	# BDD Alarms
-14.8	-14.8	0
35.2	36.2	0
85.2	86.7	0
135.2	137.5	0
185.2	Non convergent	-

Bad Data Detected & Removed

- Stealth attack of 150 MW ($\approx 55\%$ of nominal value) passed undetected in testbed!

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Min Cut Algorithm on the Board

Compare:

“Hard”:

$$\begin{aligned} & \underset{\Delta\theta \in \mathbb{R}^{n+1}}{\text{minimize}} && c^T g(DA^T \Delta\theta) + p^T g(ADA^T \Delta\theta) \\ & \text{subject to} && A(:, \bar{e})^T \Delta\theta \neq 0 \end{aligned} \tag{1}$$

“Easy”:

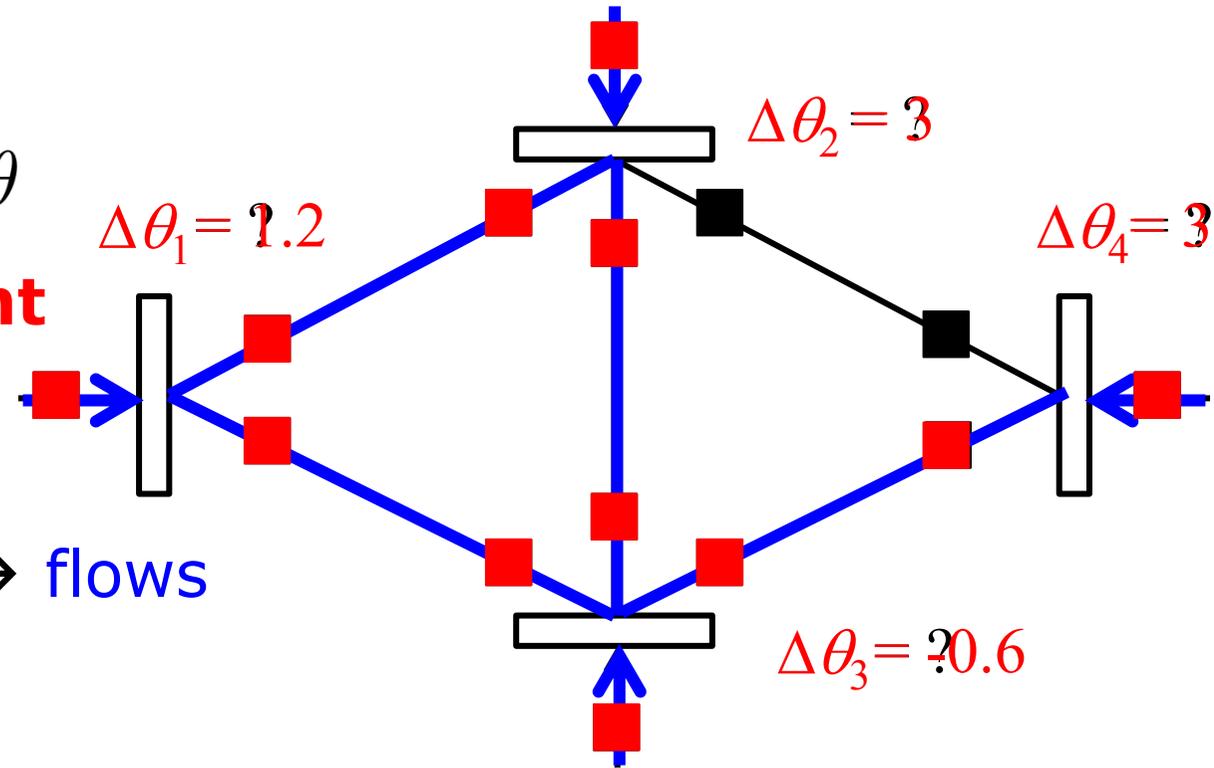
$$\begin{aligned} & \underset{\Delta\theta \in \{0,1\}^{n+1}}{\text{minimize}} && c^T g(DA^T \Delta\theta) + p^T g(ADA^T \Delta\theta) \\ & \text{subject to} && A(:, \bar{e})^T \Delta\theta \neq 0. \end{aligned} \tag{2}$$

[Theorem 1, Hendrickx *et al.*, IEEE TAC, 2014]

Graph Interpretation of Stealth Attack

Stealth attack $\Delta z = H \Delta \theta$
 = **phase angle assignment**

Phase angle differences \rightarrow flows



attack cost $\text{card}(H \Delta \theta) =$ **# of meters with nonzero flows**

Binary Phase Assignment is Optimal

Security index problem

$$\min_{\Delta\theta} \text{card}(H\Delta\theta)$$

s.t.

$$H(k, :)\Delta\theta = 1$$



[Sou *et al.*, CDC, 2011]

[Hendrickx *et al.*,
 IEEE TAC, 2014]

$$\min_{\Delta\theta} \text{card}(H\Delta\theta)$$

s.t.

$$H(k, :)\Delta\theta = 1$$

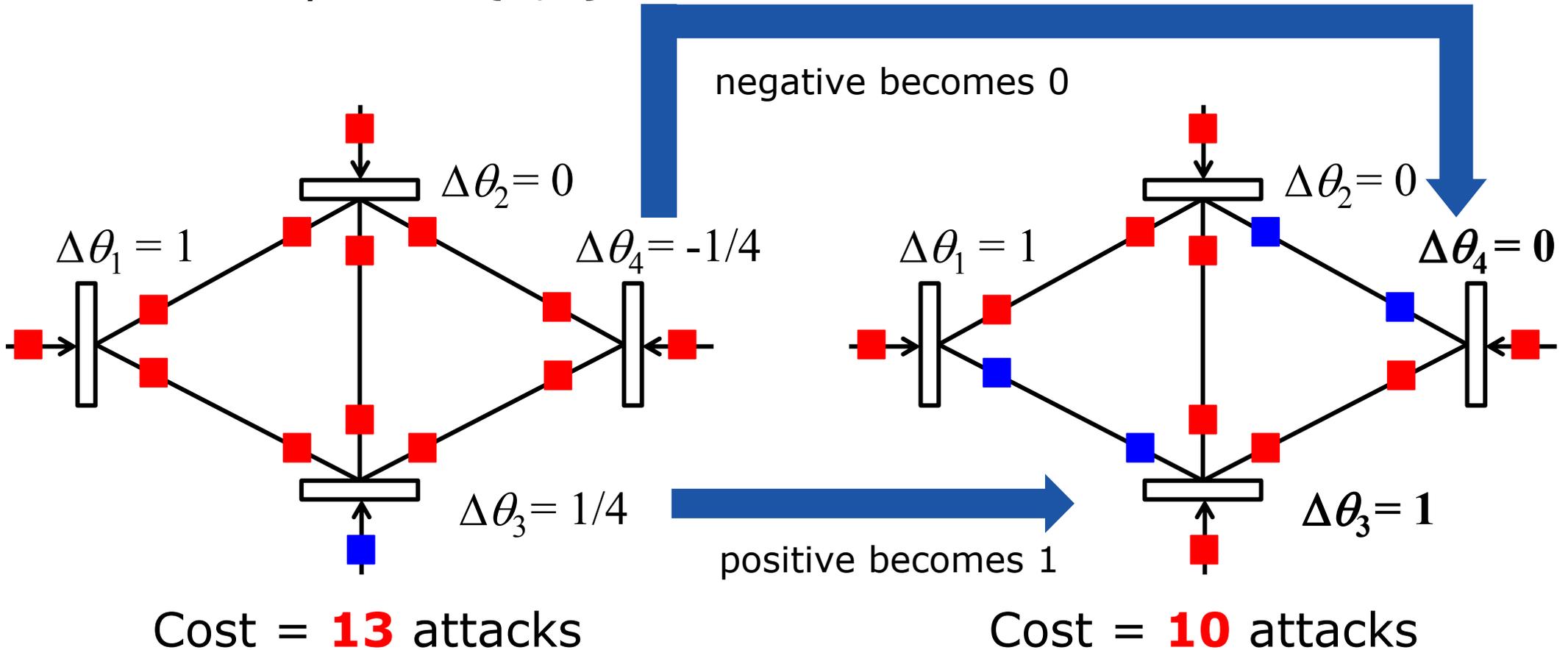
$$\Delta\theta_i \in \{0, 1\}$$

Theorem: Optimal $\Delta\theta_i$ can be restricted to 0 or 1, for all i

Proof: Restriction can never increase number of flows,
 given the structure of H

Binary Optimal Solution Justification

Can always find $\{0,1\}$ feasible solution with no worst cost

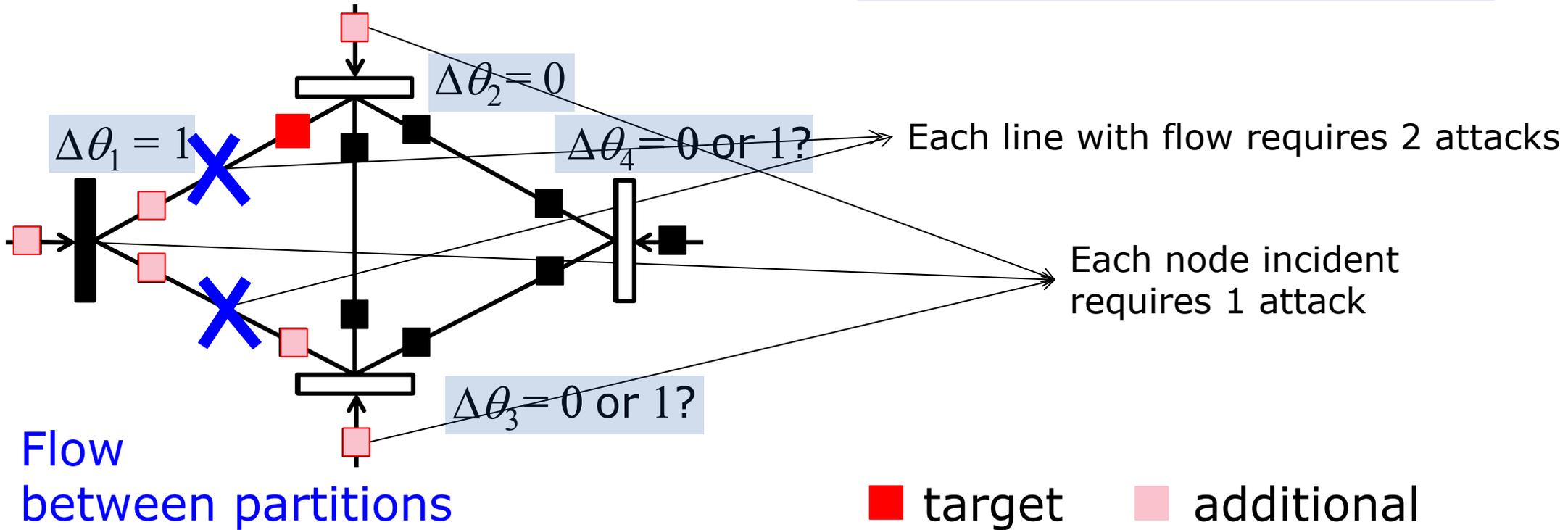


Reformulation as Node Partitioning

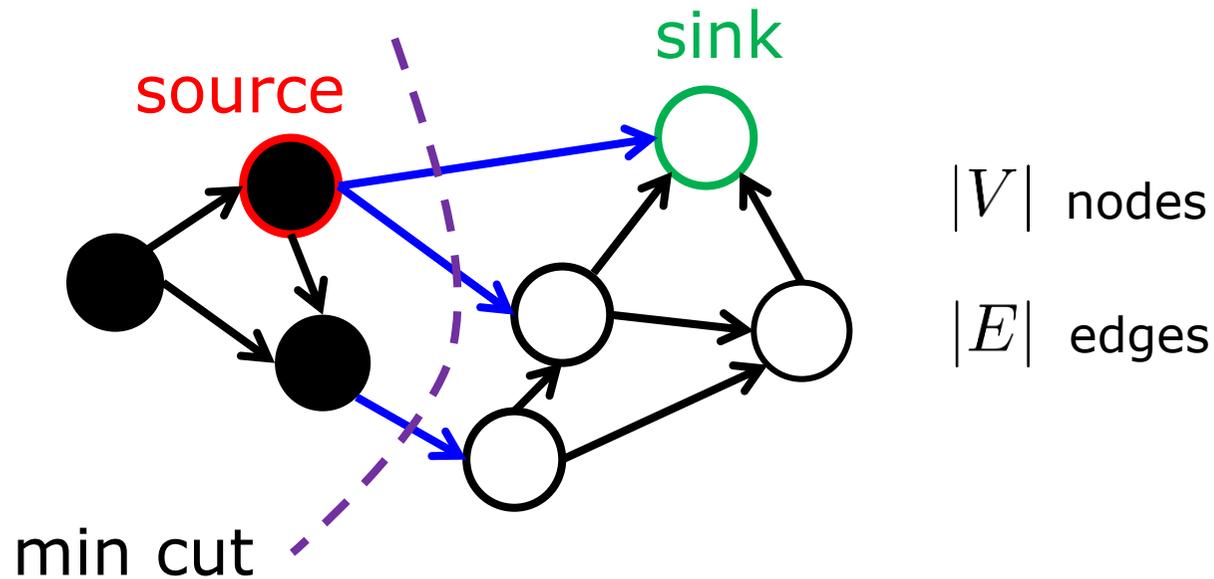
$$\begin{aligned} & \min_{\Delta\theta} \text{card}(H\Delta\theta) \\ & \text{s.t. } H(k, :)\Delta\theta = 1 \\ & \Delta\theta_i \in \{0, 1\} \end{aligned}$$



Security index problem:
Pick partition of minimum # of flows and incident nodes



Interlude: The Min Cut Problem

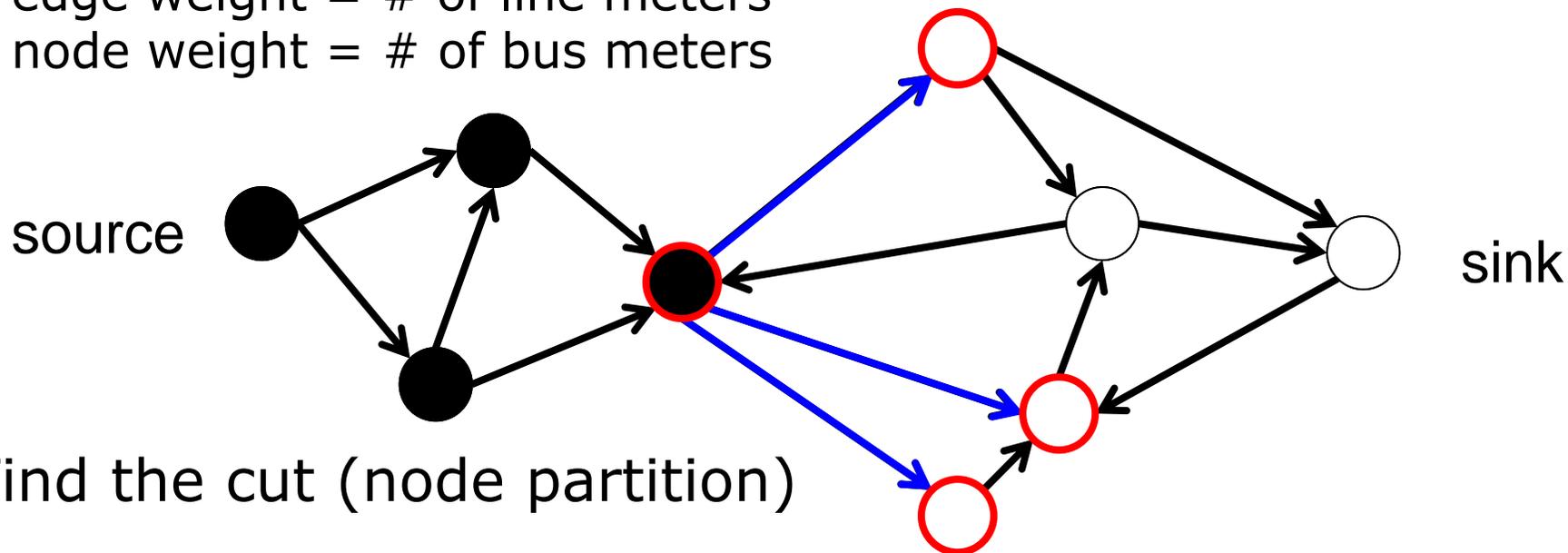


- Partition nodes into two sets (**black** and white) such that **source** is **black** and **sink** is white (“a cut”)
- Find partitions with the smallest number of edges from source set to sink set (“a min cut”)
- Problem solvable in $O(|V||E| + |V|^2 \log(|V|))$ operations

Generalized Min Cut with Costly Nodes

Focus on directed graph (undirected = bi-directed)

edge weight = # of line meters
node weight = # of bus meters



Find the cut (node partition)

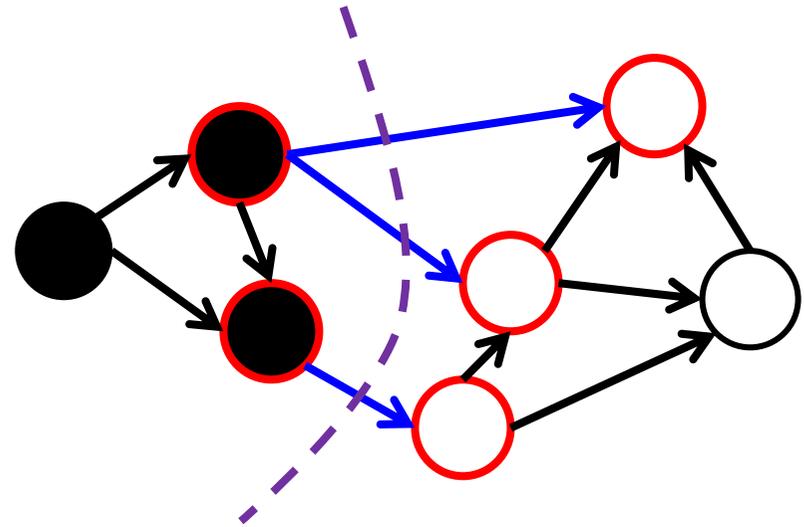
to minimize weights of cut **edge** + incident **node** weights...

Generalization of standard Min Cut!

Security index problem

Generalized Min Cut problem

$$\begin{aligned} \min_{\Delta\theta \in \mathbb{R}^{n+1}} \text{card}(H\Delta\theta) \\ \text{s.t. } H(k, :) \Delta\theta = 1 \end{aligned}$$



How to solve generalized Min Cut?

Standard Min Cut on Appended Graph

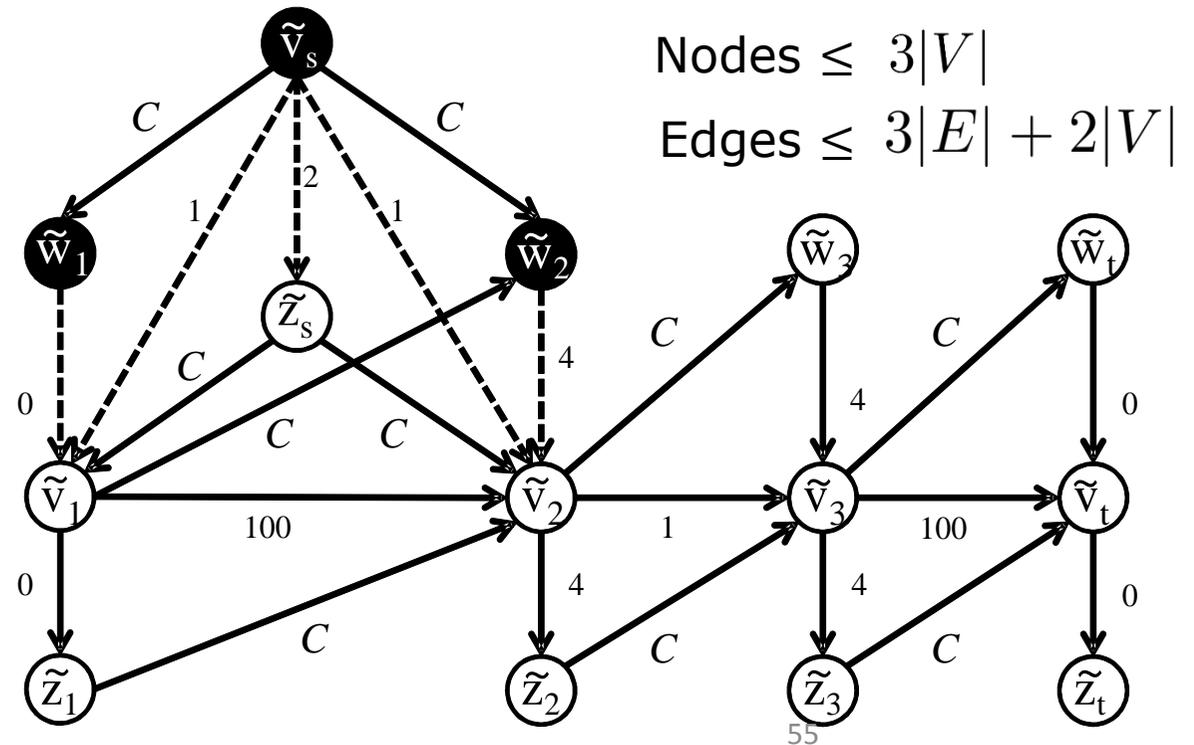
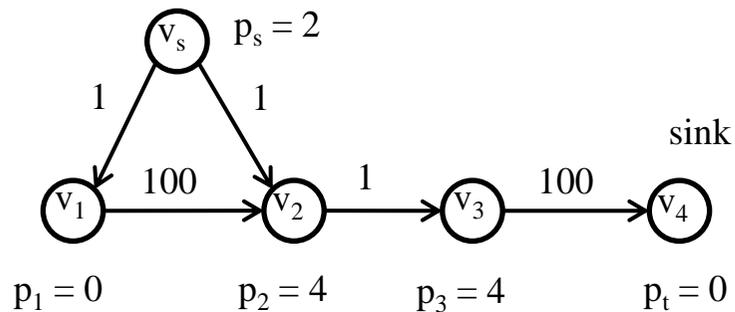
Generalized Min Cut = Standard Min Cut on **appended** graph

generalized min cut \longleftrightarrow standard min cut appended graph

$|V|$ nodes

$|E|$ edges

source



Nodes $\leq 3|V|$

Edges $\leq 3|E| + 2|V|$

[Hendrickx *et al.*, IEEE TAC, 2014]

$$C > \max_i p_i$$

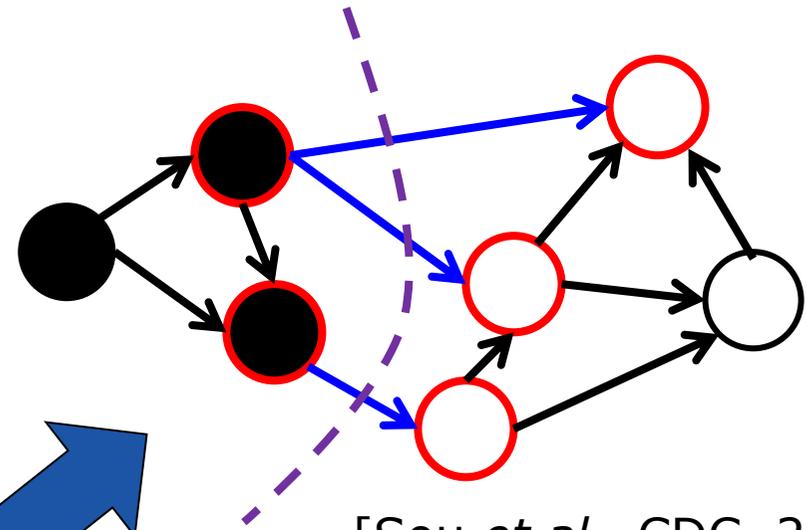
Security Index Problem – Summary

Security index problem

$$\min_{\Delta\theta} \text{card}(H\Delta\theta)$$

$$\text{s.t. } H(k, :)\Delta\theta = 1$$

Generalized Min Cut problem



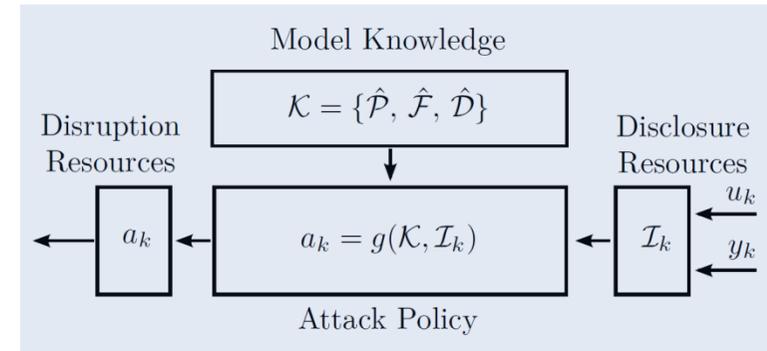
[Sou *et al.*, CDC, 2011]
[Hendrickx *et al.*, TAC, accepted 2014]

Standard Min Cut problem
on an **appended** graph

>> [maxflow, mincut] = max_flow(A, source, sink);

Summary

- Cyber threats in control systems
- Adversary model in control systems



- A security metric for state estimators and its computation using Min Cut

$$\begin{aligned} & \min_{\Delta\theta} \text{card}(H \Delta\theta) \\ & \text{s.t. } H(k, :) \Delta\theta = 1 \end{aligned}$$

- Exercises: Compute and understand the security metric
- Tomorrow: Attack space for cyber-physical systems